

[Click to see animation of fracture simulation.](#)

Numerical Simulation of Reservoir Structures, Part II: Propagation of a Pressurized Fracture in Rock Layers with Damage Rheology*

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Search and Discovery Article #40484 (2010)
Posted February 19, 2010

*Adapted from oral presentation at AAPG Convention, Denver, Colorado, June 7-10, 2009. Please refer to closely related articles by [Seth Busetti and co-workers: Numerical Simulation of Reservoir Structures, Part I: Rheology of Reservoir Rocks](#), Search and Discovery article #40483 (2010), and [Numerical Simulation of Reservoir Structures, Part III: Folding of a Layered Rock Sequence in a Ramp System](#), Search and Discovery article #40485 (2010).

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Abstract

We use finite element simulations to study the effect of local geologic conditions during hydraulic fracturing of rock layers with damage rheology. This work is part of our study on structural processes in reservoir rocks using numerical simulations with the code Abaqus. [Part I](#) (Busetti et al.) covers rock rheology and benchmark simulations, and [Part III](#) (Heesakkers et al.) studies the role of visco-plastic rheology on ramp induced thrust-folding.

Hydraulic fractures frequently propagate through multiple layers of naturally fractured rock, each with distinct stress state and material properties. Thus, we examine fracture propagation as a function of mechanical properties of the host and neighboring layers, layer dimensions, tectonic stress state, and internal pressure. We model a wellbore-scale section of layers with frictional contacts located away from near-borehole effects. Beds of high elastic modulus and yield strength reflect potential “fracture barriers”. Rheology is for elastic-plastic damaged rock based on experiments of Berea Sandstone, Indiana Limestone, and Barnett Shale (see Part I). We first investigated the up-section propagation of a vertical hydrofracture 0.25 m tall, embedded in a 0.3 m host layer, overlain by 1 to 8 horizontal layers from 0.125 to 1 m thick. We establish tectonic stresses for depths of ~2.5 km and then apply increasing pressure (0 - 100 MPa) to viscous fluid in the fracture to simulate a single injection stage.

The results suggest that the model parameters are interrelated. We found the following parameters reduce the tendency to propagate fractures: (1) thinner layers; (2) lower inter-layer friction; (3) higher vertical stress; (4) higher elastic modulus ratio between the host and overlying layers. Higher stress ratio ($S_v > S_h$) increased the tendency for longer fractures; lower stress ratio ($S_v \approx S_h$) increased the tendency for multiple sub-vertical fractures. The models indicate that interlayer slip is a strong mechanism to locally accommodate pressurization strain. We anticipate that slip along preexisting fractures and bedding planes could redirect flow along diffuse fracture patterns. The simulations indicate that to predict propagation of hydrofractures, one should consider fracture interaction with preexisting structures and their local stress. Future models will explore the effect of fracture inclination as well as growth in three dimensions.

Acknowledgement

This work is supported by funds from ConocoPhillips.

Selected References

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Numerical Simulation of Reservoir Structures, Part II: Propagation of a Pressurized Fracture in Rock Layers with Damage Rheology

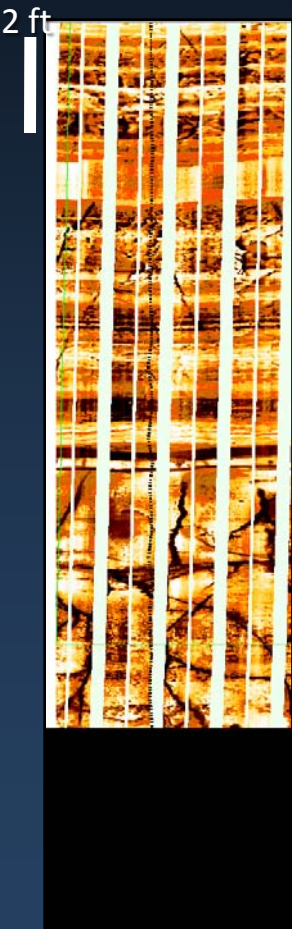
Seth Buseti and Ze'ev Reches
University of Oklahoma

June 2009

Hydraulic Fracturing in Tight Reservoir Rocks

Actual geologic conditions are quite complex...

...actual hydraulic fractures are equally complex...



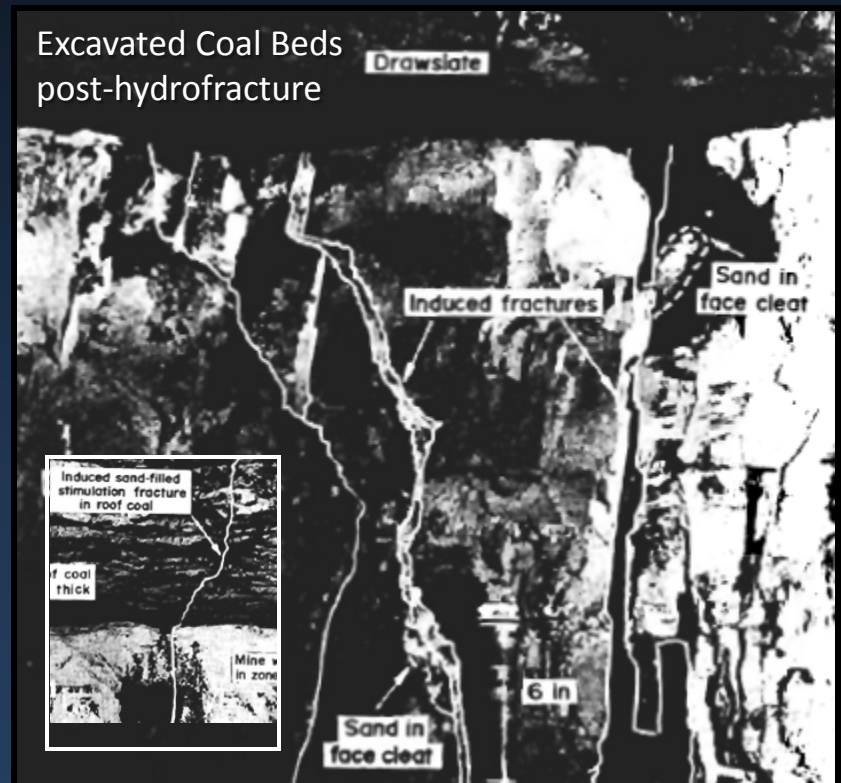
Heterogeneous Reservoir Rock,
Alternating Barnett Shale Lithologies



Barnett Shale, TX

[*http://www.geo.utexas.edu/scientist/milliken/barnettshale.htm](http://www.geo.utexas.edu/scientist/milliken/barnettshale.htm)

Heavily Fractured, Water-Bearing
Ellenberger Limestone



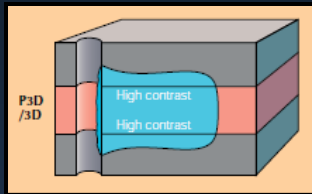
Bureau of Mines, 1977

Goal: Understanding the process
under in-situ geologic conditions

Models for Hydrofracturing – Geologic Complexity

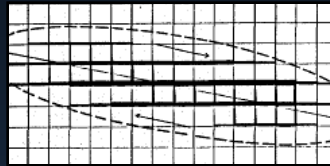
“Geometric Models”

Simple Rheology
Simple Propagation
No Interactions



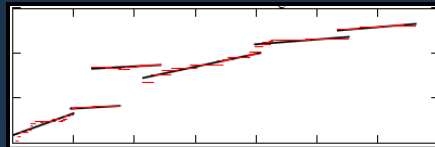
Brady et al. 1992

Simple Rheology
Simple Propagation
Simple Interactions



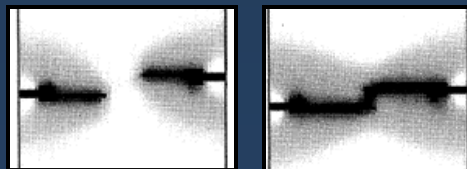
Murphy et al., 1988

Simple Rheology
Complex Propagation
Complex Interactions



Sim 2004

Complex Rheology
Simple Propagation
Complex Interactions



Weinberger et al. 2000

Rock Rheology

- Linear Elastic ^[1]
- Linear elastic, non-linear cohesive zone ^[2]
- Elastic-plastic, non-linear cohesive zone ^[3]
- Non-linear elastic, continuum damage ^[4]
- **Elastic-plastic, continuum damage ^[5]**
- Elastic-plastic, damage, fluid penetration ^[6]

[1] e.g., Hubbert and Willis, 1957; Haimson, 1967;
KGD; PKN; Radial; Desrouches et al., 1994

[2] after Barenblatt, 1962

[3] e.g., Papanastasiou, 1997

[4] Weinberger et al., 2000

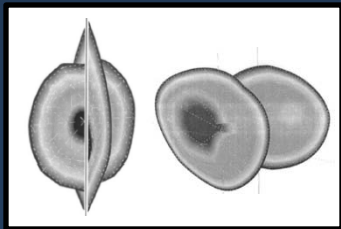
[5] **this work**

[6] future work

Our Aim is to Model:

- ✓ Complex Rheology
- ✓ Complex Interaction
- ✓ Complex Propagation

Simple Rheology
Complex Propagation
No Interactions



Yamamoto et al. 2004

Scope of the Study

Tectonic Stress State

- ✓ 2D Plane Strain

Scale

Far Field (geologic conditions)

- ✓ Single layer (1s meters)



Simulation Time

- ✓ Short Duration

Layer Properties

(*Rheology, Geometry)

- ✓ Isotropic Host Layer

Fracture Interactions

- ✓ Fracture Propagation
- ✓ Fracture Pattern

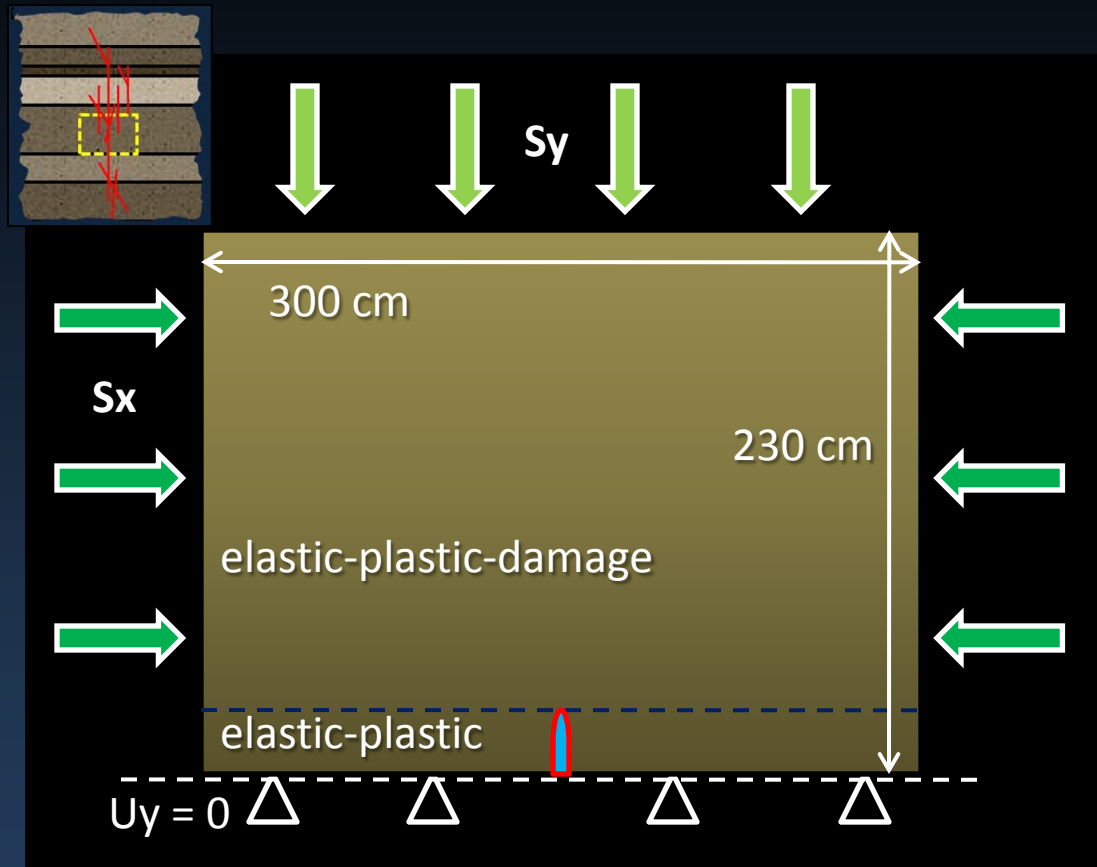
Fluid Properties

- ✓ Internal Pressure
- ✓ Pressure Distribution

*Part I



FEM Model Configuration



Finite Element Analysis:
 2D plane strain
 explicit dynamic solver (Abaqus/Explicit)
 2680 linear quad/tri elements

Tectonic Loading:

$S_y = 50 \text{ MPa}$

$S_x = 10\text{-}45 \text{ MPa}$

Pressure Loading:

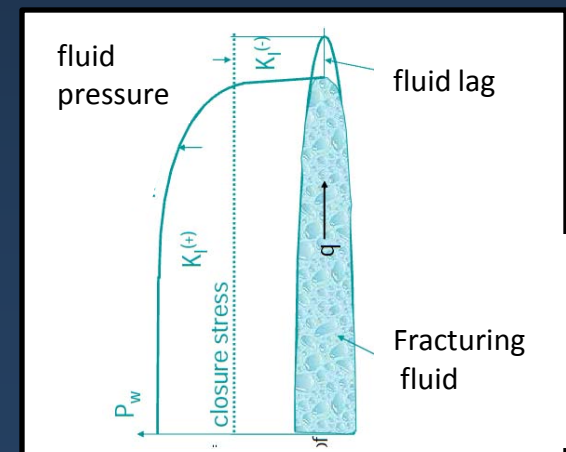
No fluid penetration

$P_f(t)$ = linear increase

(a) constant pressure

(b) non-linear distributed pressure:

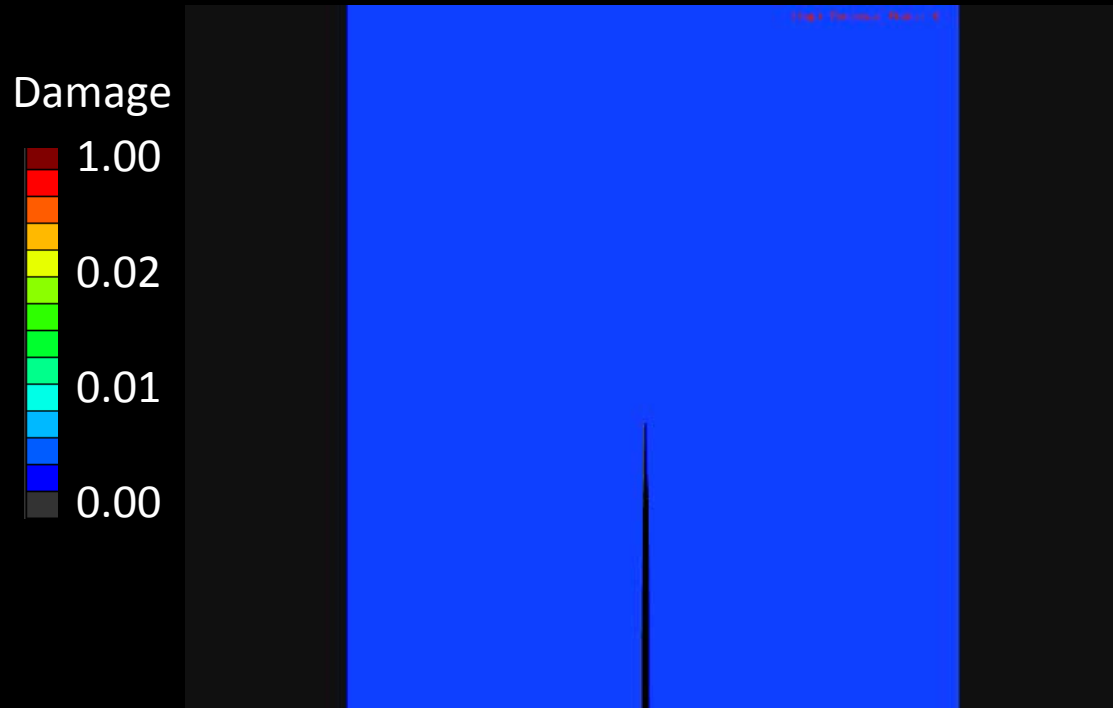
$$dp/dx = 12\mu q/w^3$$



Modified from Papanastasiou, 2002

Hydraulic Fracture Propagation Simulation

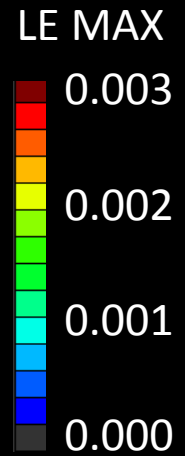
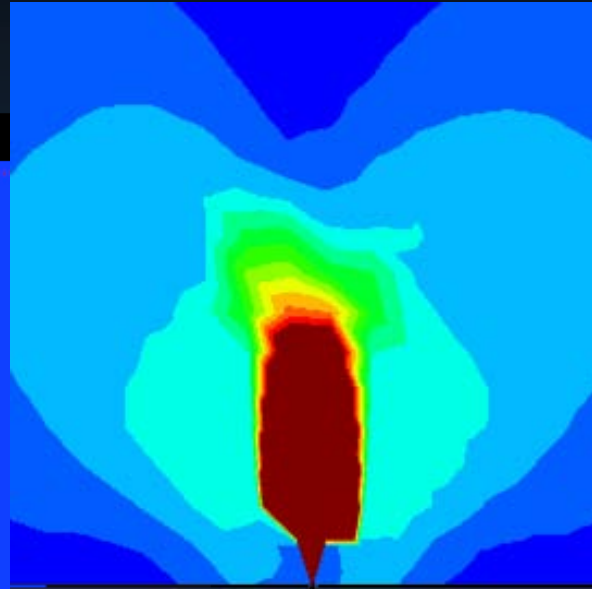
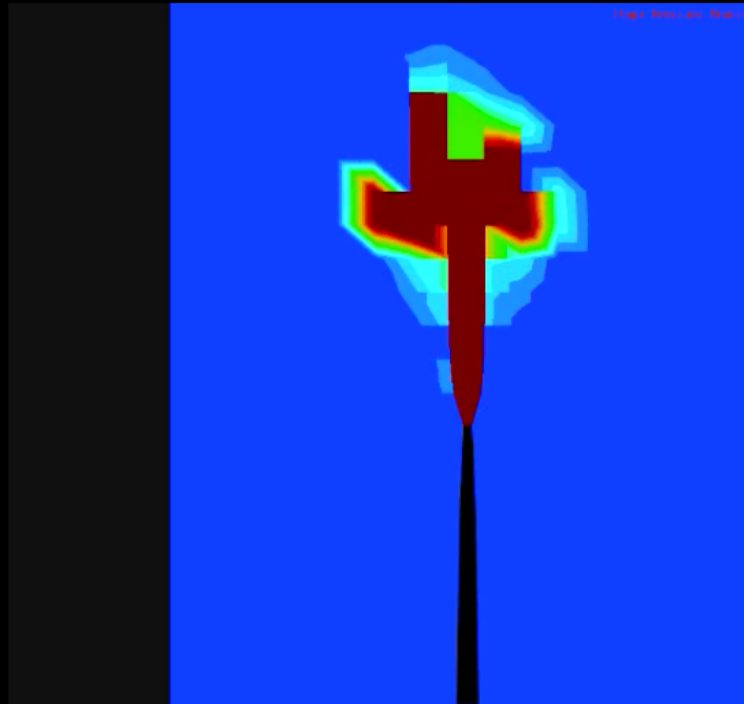
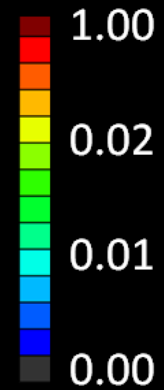
20x 50y $dp/dx=0$



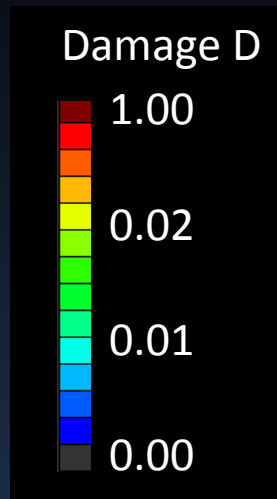
Hydraulic Fracture Propagation Simulation

20x 50y $dp/dx=0$

Damage



Main Features



Failed Branches

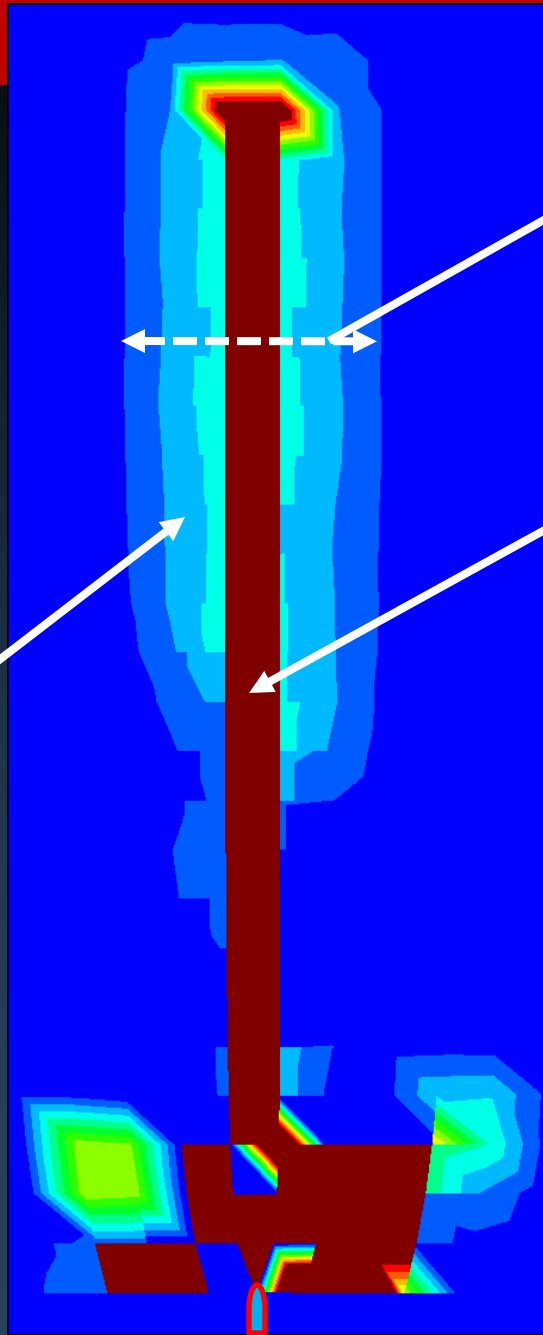
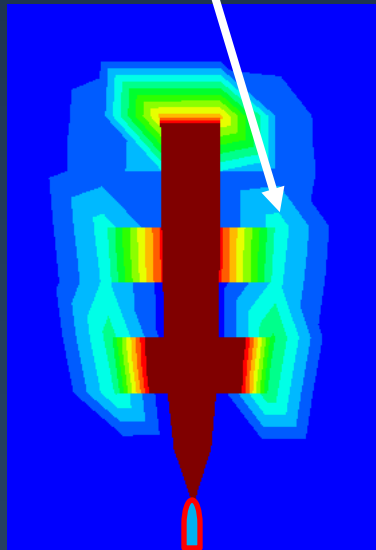
Damage Corridor

Main Fracture Path

Stable:
 $S_x > S_y$

Unstable:
 $S_x \gg S_y$

Cases Shown: Extension Only
($P = 0$)

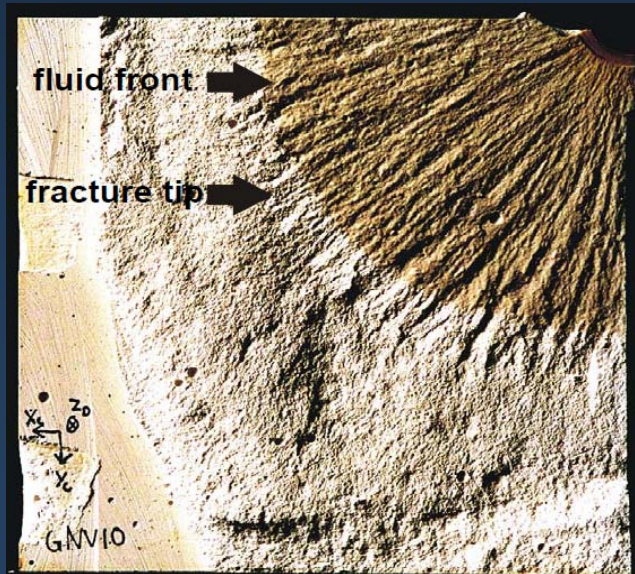
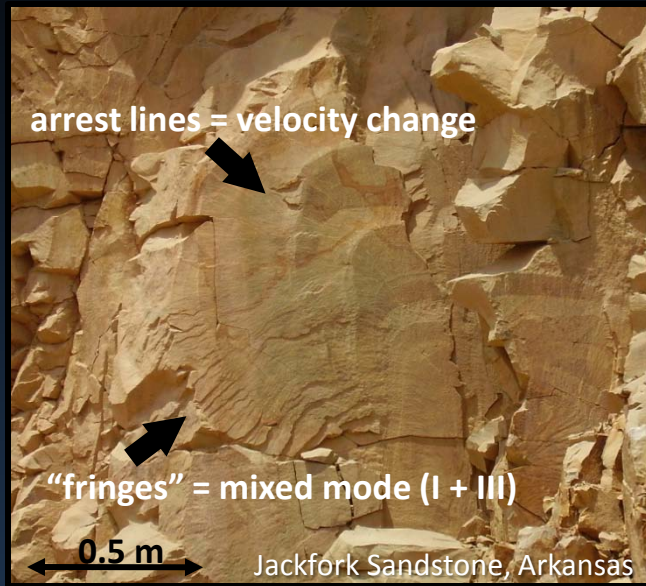


Hydraulic Fracture Simulations: Analysis / Discussion

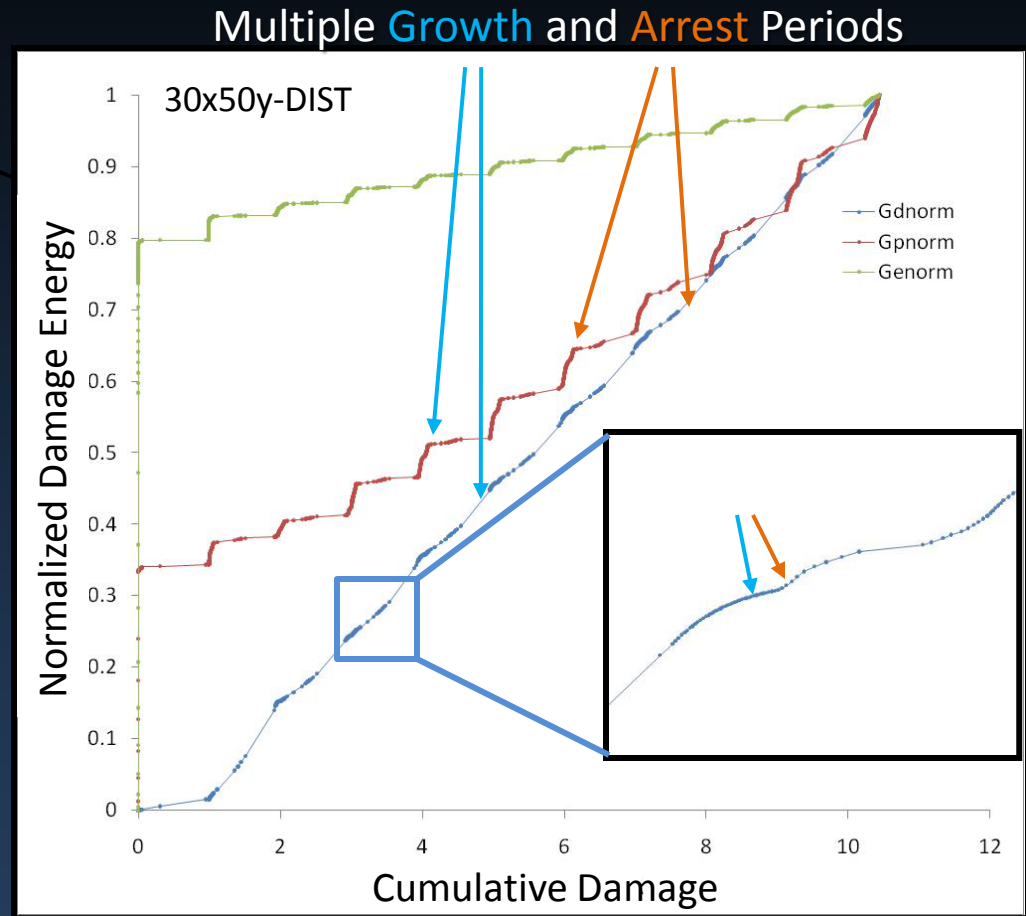
Discussion of Simulations – Highlights

1. Fracture Morphology
 - a. Fracture arrest and rupture
 - b. Segmentation and branching
 - c. Fracture velocity and stability (*not discussed here*)
2. Conditions Controlling Propagation
 - a. Tectonic load / fluid pressure
 - b. Fluid pressure distribution (*not discussed here*)
3. Example Reservoir Application

1a. Morphological Features: Fracture Arrest and Rupture



DelFrac Experimental Hydrofrac (Papanastasiou, 2002)



Cumulative (global) pattern shows build-up and release periods, \approx stable or unstable fracture growth.

This is related to local dynamical behavior...

1b. Morphological Features: Branching and Segmentation



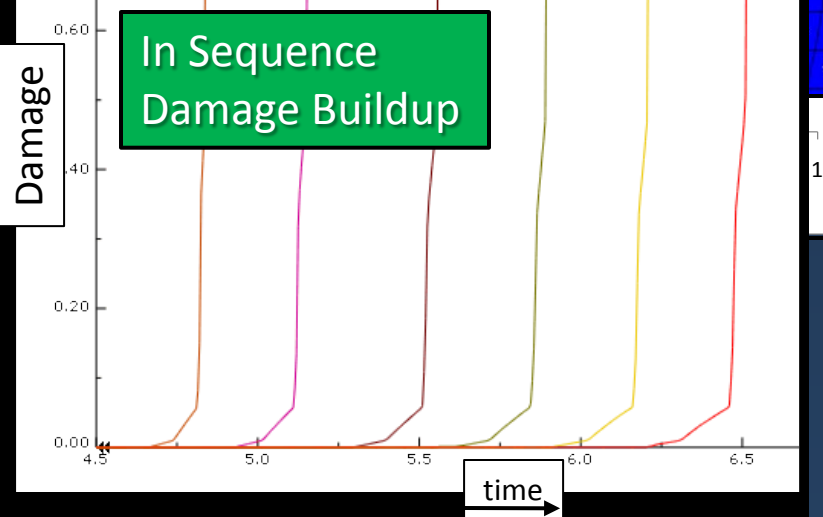
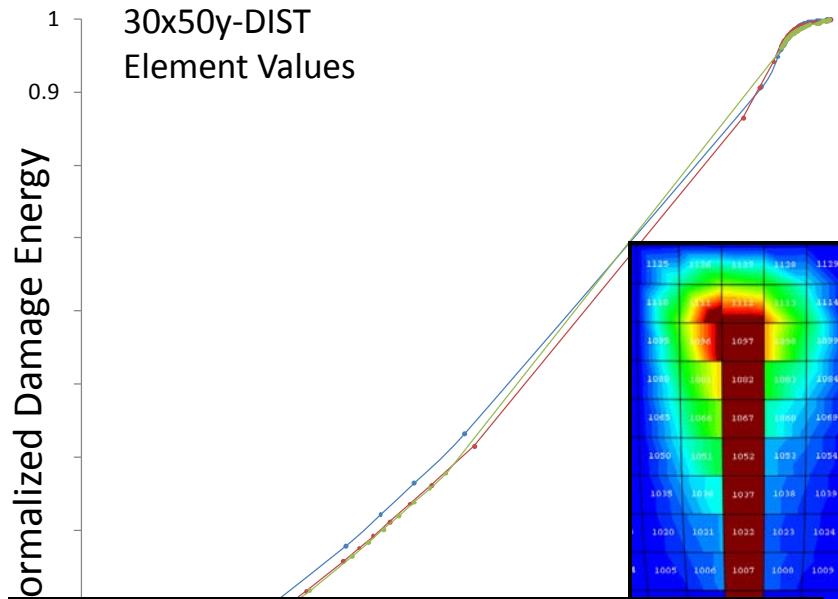
Jackfork Sandstone, Ouachitas, Arkansas



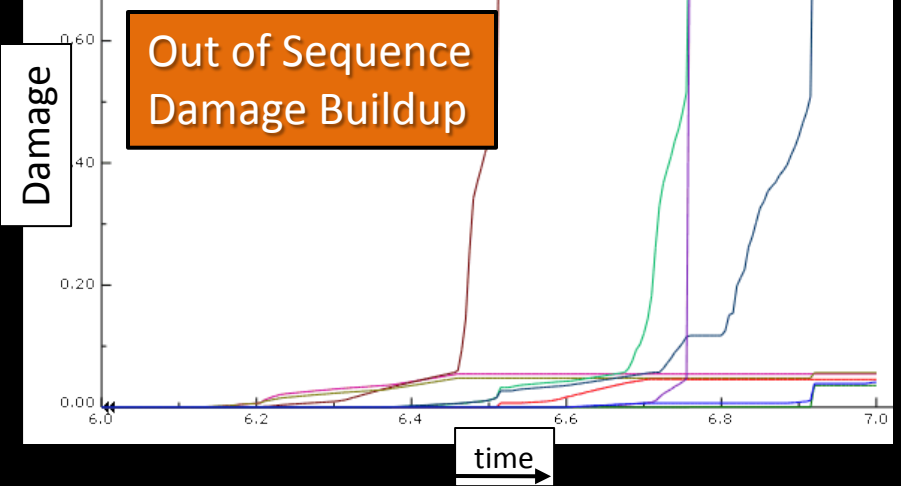
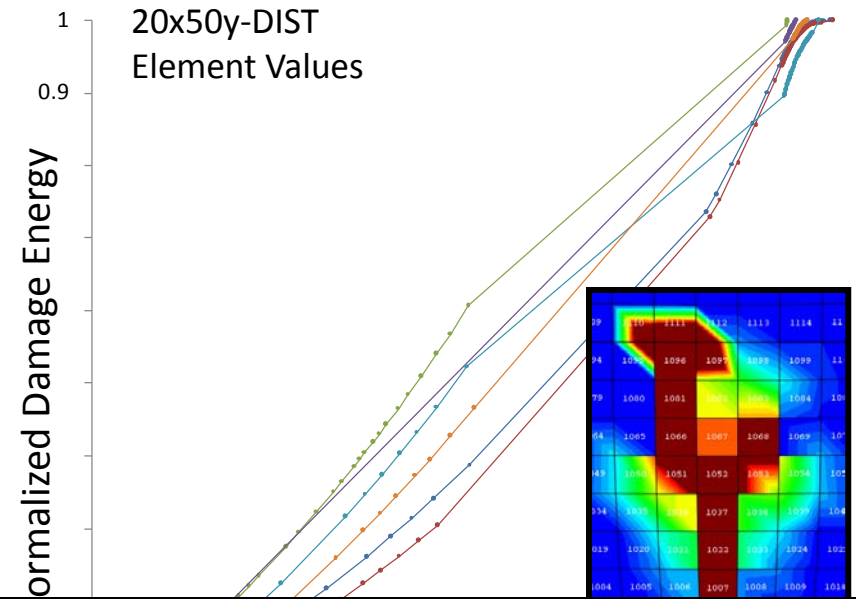
Carmel Fm. Limestone, Cedar Mountain, Utah

1b. Morphological Features: Segmentation and Branching

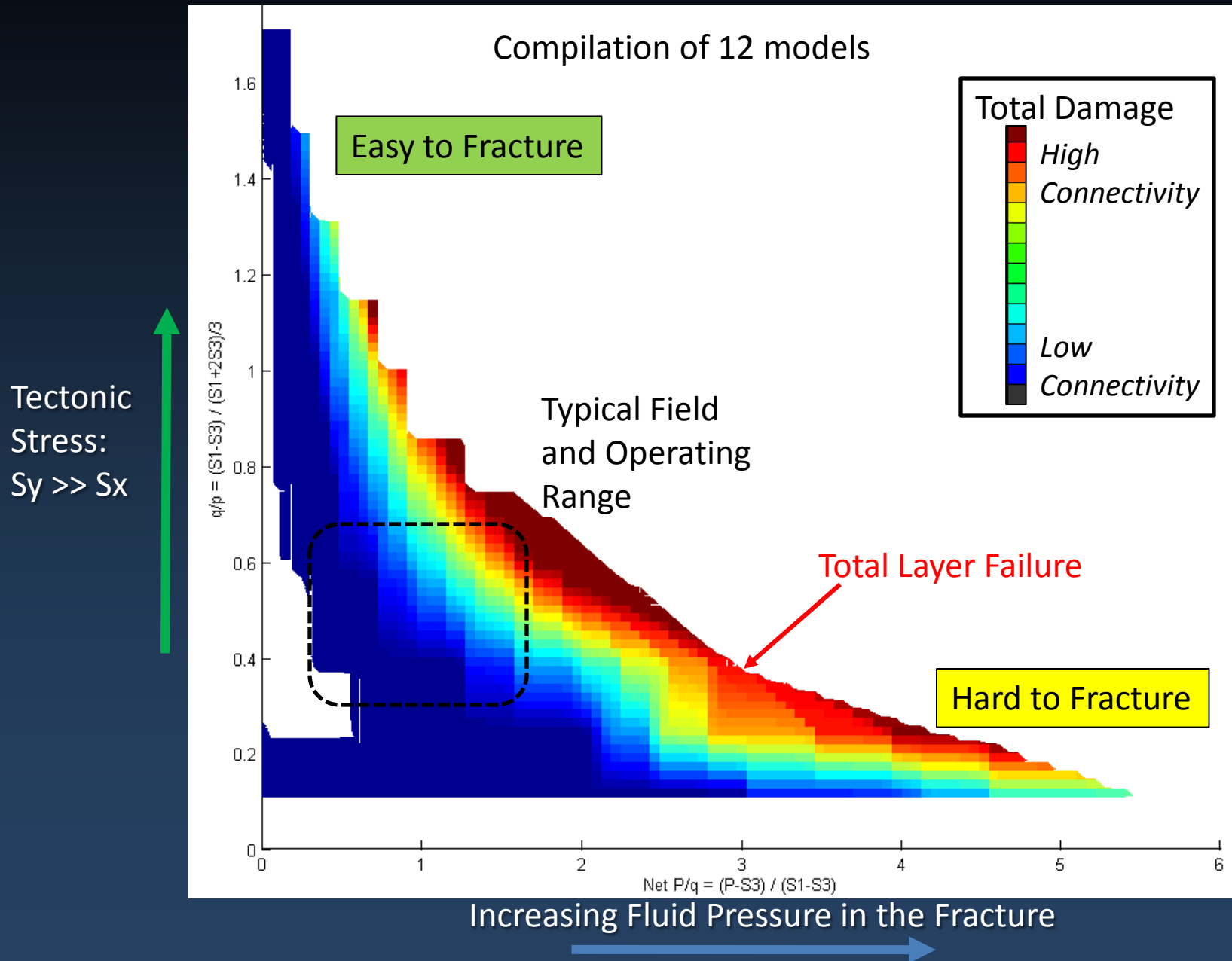
Simple Fracture



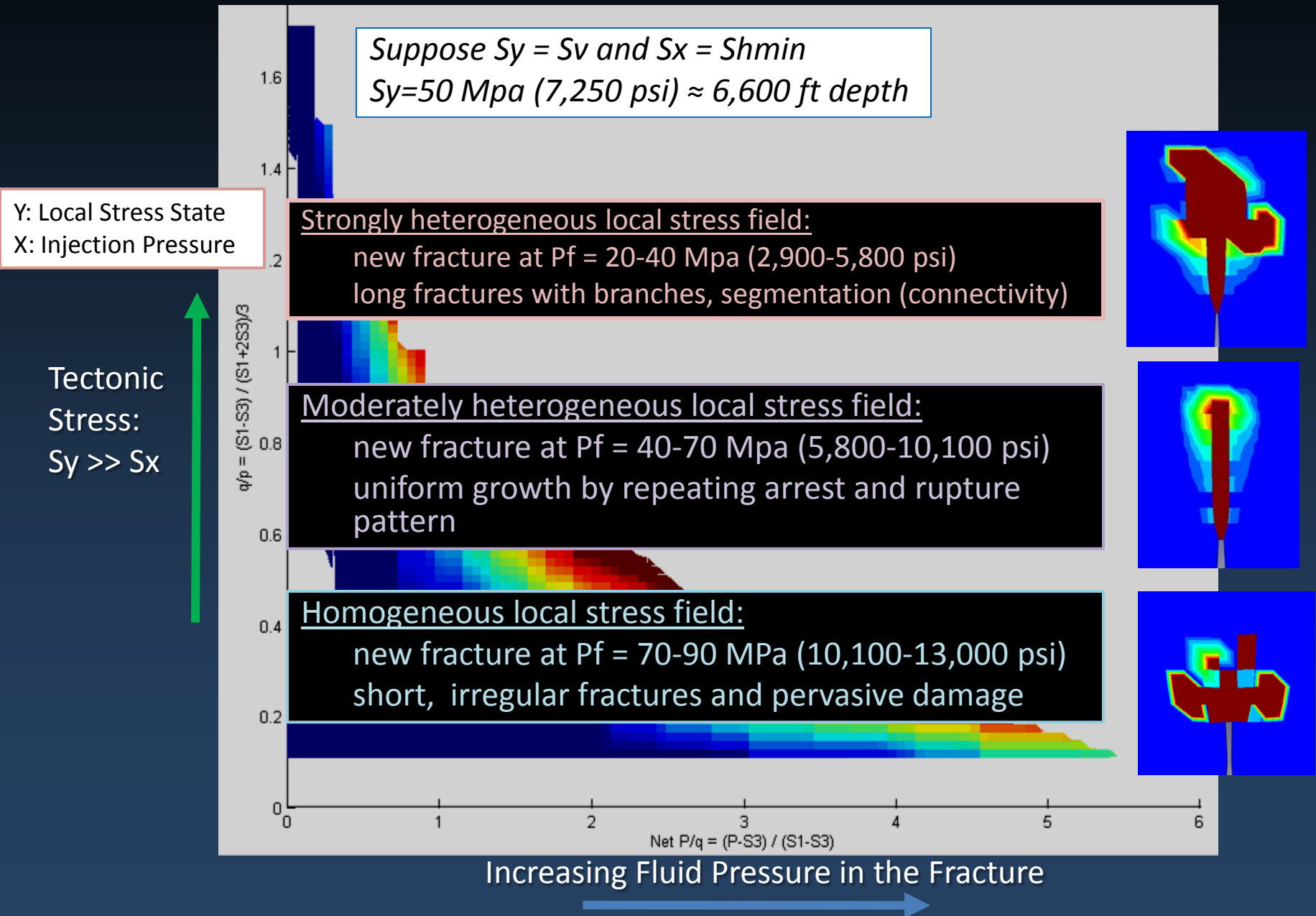
Complex Fracture



2a. Damage as a Function of Tectonic and Fracture Pressure



3. Example Reservoir Application



Summary

Approach / Rationale

Use explicit/dynamic FEM simulations and elastic-plastic-damage rheology
(covered in Part I)

Failure criteria for compression and tension

Dissipative processes: brittle microcracking damage, plasticity

Non-local complex rheology: damage and failure outside the crack-tip zone

Results

The elastic-plastic-damage rheology yields:

- Development of branches and segments that are associated with strain build-up periods, which tend to cause broader zones of damage

- High sensitivity to loading conditions:

 - Fracture Morphology*

 - Fracture Evolution*

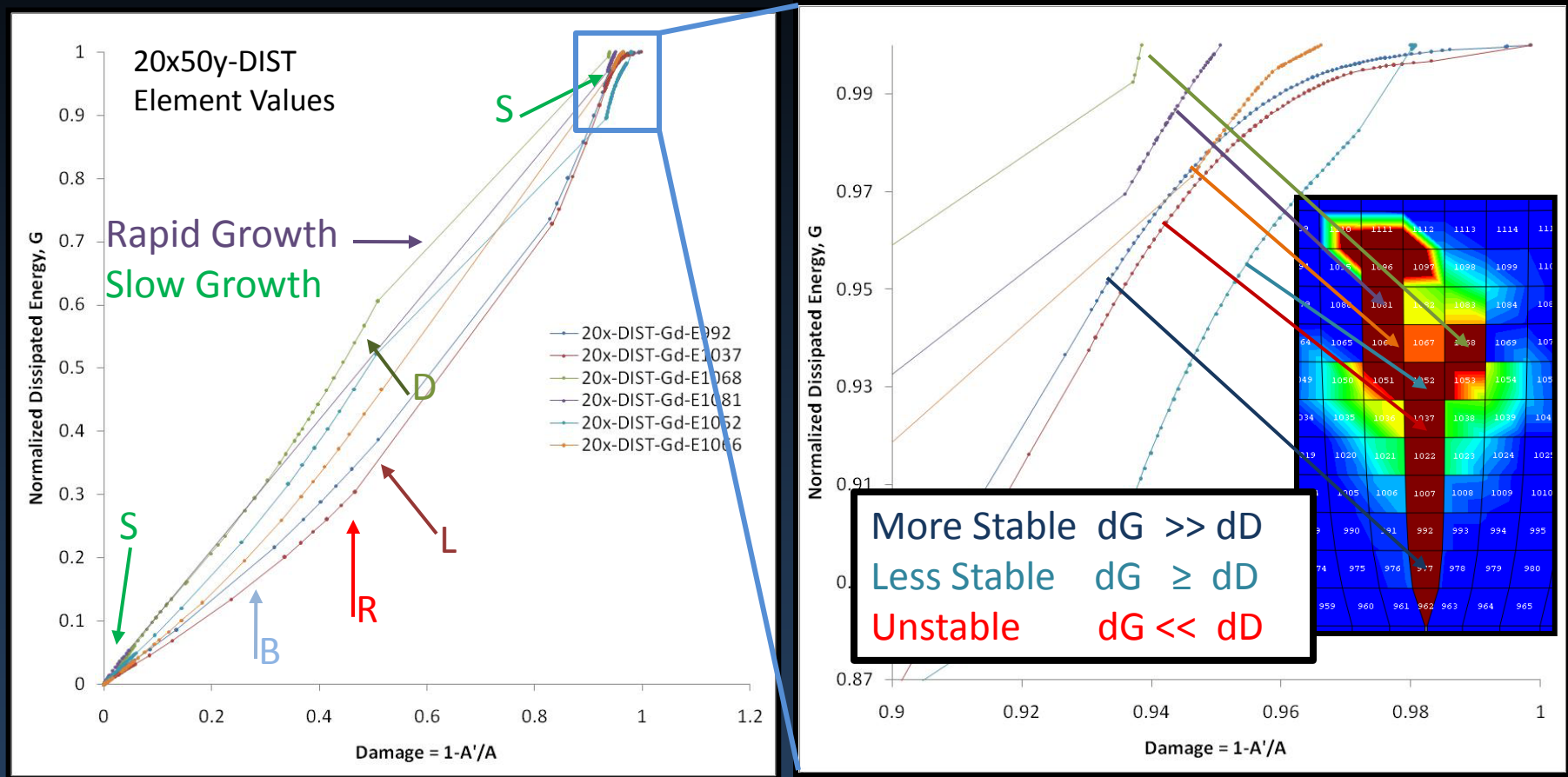
 - Distributed Damage = Connectivity*

- Shows potential for reservoir analysis:

 - Continued analysis of Barnett Shale field data

Backup slides

2c. Dynamical Features: Fracture Velocity and Stability



Buildup – damage accumulation \rightarrow Localized ($dG/dD \downarrow$) \rightarrow in-plane (simple)
 Diffuse ($dG/dD \uparrow$) \rightarrow out-of-plane (complex)

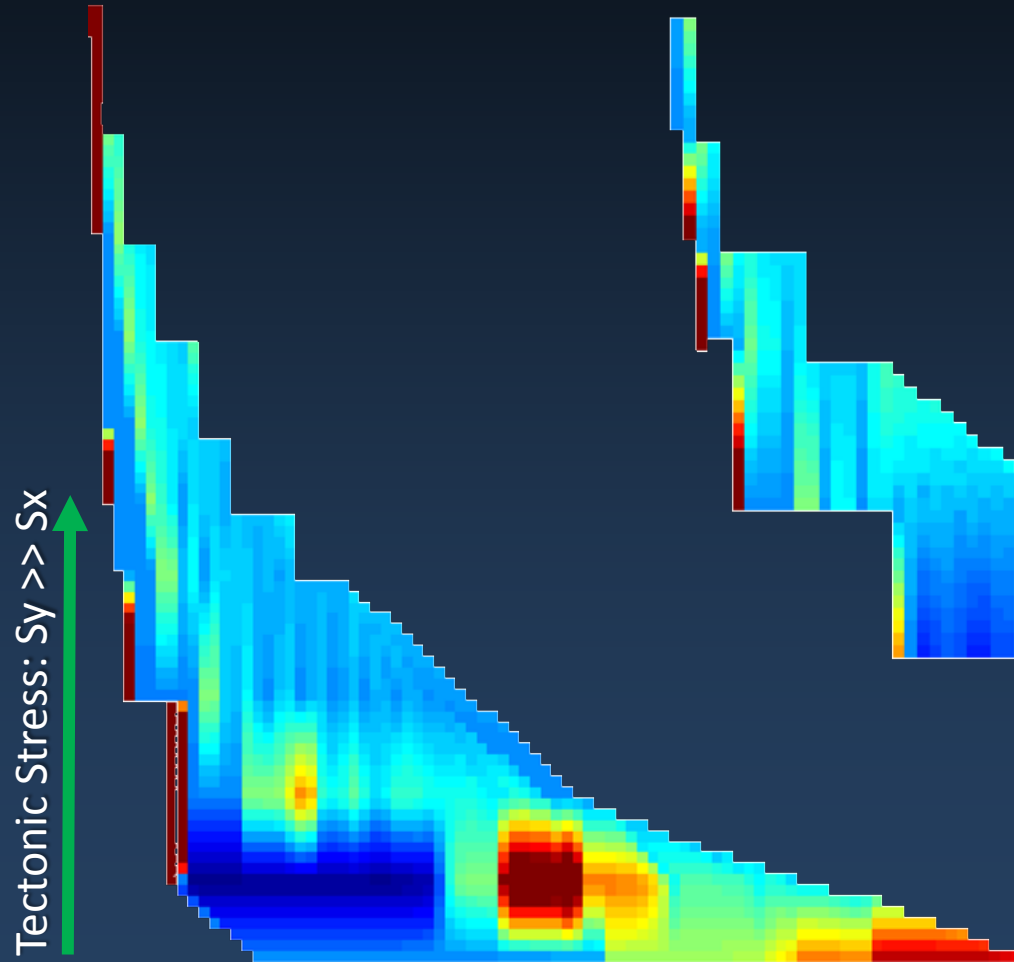
Rupture – ultimate yield and softening

Arrest – post-failure damage zone transference \rightarrow Localized \rightarrow self-similar, planar
 Diffuse \rightarrow unique, segments/branches

2b. Controls: Fluid Pressure Distribution

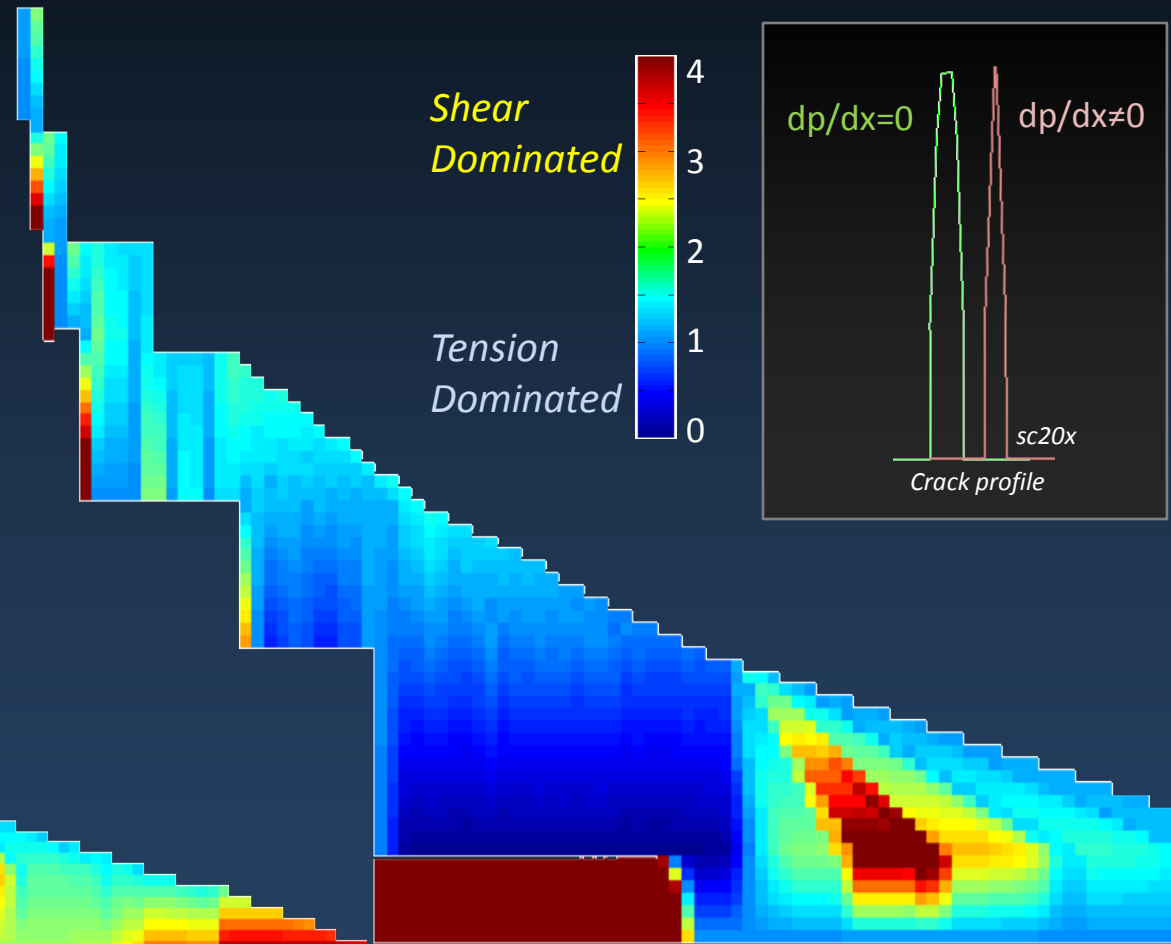
Uniform Pressure Distribution

Ratio D_c/D_t



Non-linear Pressure Distribution

Ratio D_c/D_t



Hydraulic Fracturing in Tight Reservoir Rocks

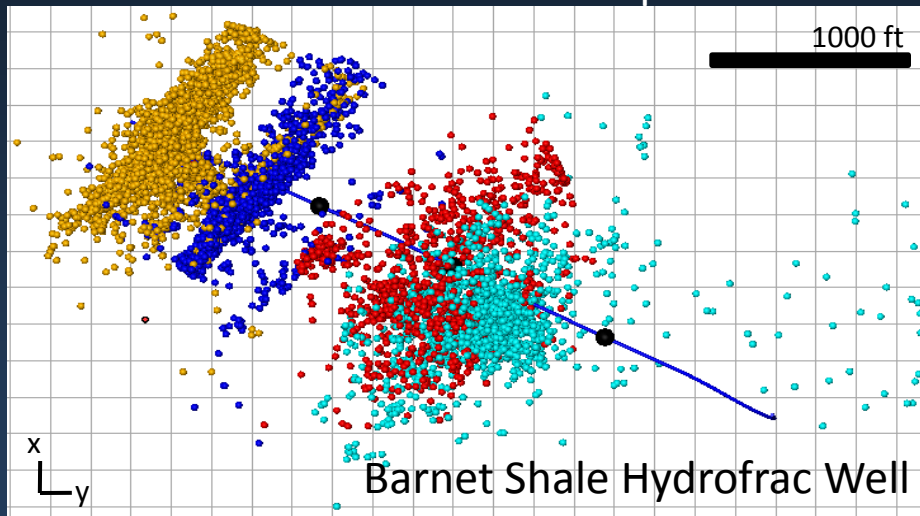
Purpose

Create new fracture volume
Increase fracture connectivity
Stimulate fluid flow

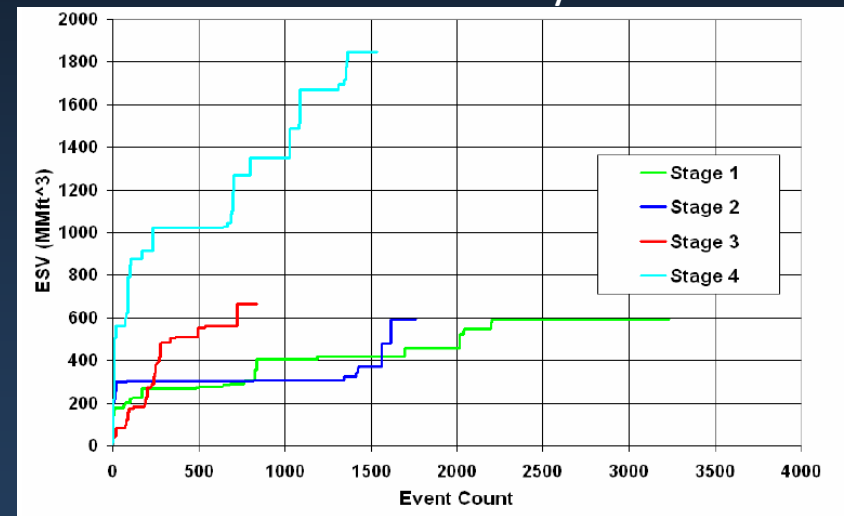
Observation Technique

Microseismic, Fluid Volume Analysis
Chemical Tracers, Well Connectivity
Production Data

Microseismic Events Map



Fluid Volume Analysis



Modified from Daniels et al. 2007