

# **Saturation-Dependent Relative Permeability in Shales Based on Adsorption-Desorption Isotherm\***

**Shiv P. Ojha<sup>2</sup> and Siddharth Misra<sup>1</sup>**

Search and Discovery Article #41985 (2017)\*\*

Posted January 30, 2017

\*Adapted from oral presentation given at AAPG 2016 Eastern Section Meeting, Lexington, Kentucky, September 25-27, 2016

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## **Abstract**

Relative permeability in shales is an important petrophysical parameter for purposes of accurate estimation of production rate and recovery factor, efficient secondary recovery, and effective water management. We present a method to estimate saturation-dependent relative permeability in shales based on the interpretation of the low-pressure nitrogen adsorption-desorption isotherm measurements. Relative permeability were determined for 30 samples from the gas- and oil-window of Eagle Ford and Wolfcamp shale formations. These sample have low-pressure helium porosity (LPHP) in the range of 0.04 to 0.09 and total organic content (TOC) in the range of 0.02 to 0.06. The samples were ashed to study the effects of removal of organic matter on the pore size distribution, pore connectivity, and relative permeability. The estimated irreducible water saturation and residual hydrocarbon saturation are directly proportional to the TOC and LPHP, and exhibit 15% variation over the entire range. Pore connectivity, in terms of average coordination number, decreases by 33% with the increase in TOC from 0.02 to 0.06. The estimated fractal dimension is close to 2.7 for all the samples. The estimated relative permeability of aqueous phase and that of hydrocarbon phase at a given saturation is inversely proportional to the TOC. Relative permeability curves of the hydrocarbon phase for geological samples from various depths in a 100-feet interval indicate that the hydrocarbon production rate will vary drastically over the entire interval and these variations will increase as the hydrocarbon saturations reduce in the formation. In contrast, relative permeability curves of the aqueous phase suggest limited variation in water production rate over the entire interval. Further, based on the relative permeability curves, the hydrocarbon production is predicted to be negligible for hydrocarbon saturations below 50% and the water production is expected to be negligible for water saturations below than 80%. Efforts are ongoing to use the laboratory-based estimates to predict field-scale production and recovery rates.

### **Reference Cited**

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<https://www.youtube.com/watch?v=ICh-VtEzNvk> Website accessed January 2017.

[https://commons.wikimedia.org/wiki/File:Langmuir\\_izoterma.png](https://commons.wikimedia.org/wiki/File:Langmuir_izoterma.png) Website accessed January 2017.

[https://en.wikipedia.org/wiki/BET\\_theory#/media/File:BET\\_Multilayer\\_Adsorption.svg](https://en.wikipedia.org/wiki/BET_theory#/media/File:BET_Multilayer_Adsorption.svg) Website accessed January 2017.

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# Saturation-Dependent Relative Permeability in Shales Based on Adsorption-Desorption Isotherm

**Shiv Ojha and Siddharth Misra**  
University of Oklahoma

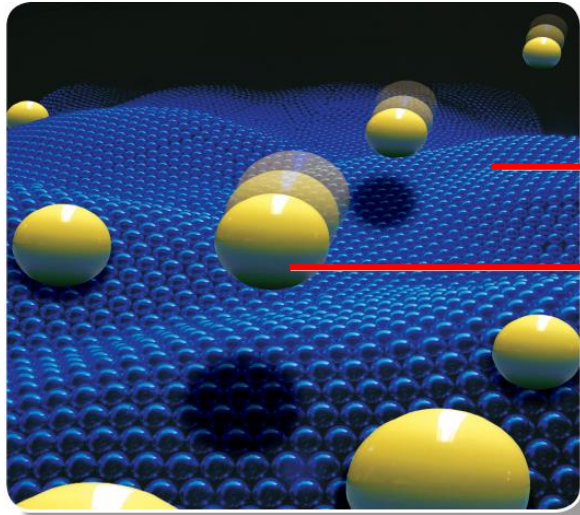
*Presenter: Siddharth Misra*



# Outline

- Introduction
- Adsorption-Desorption Measurements
- Interpretation Methodology
- Results
- Conclusions

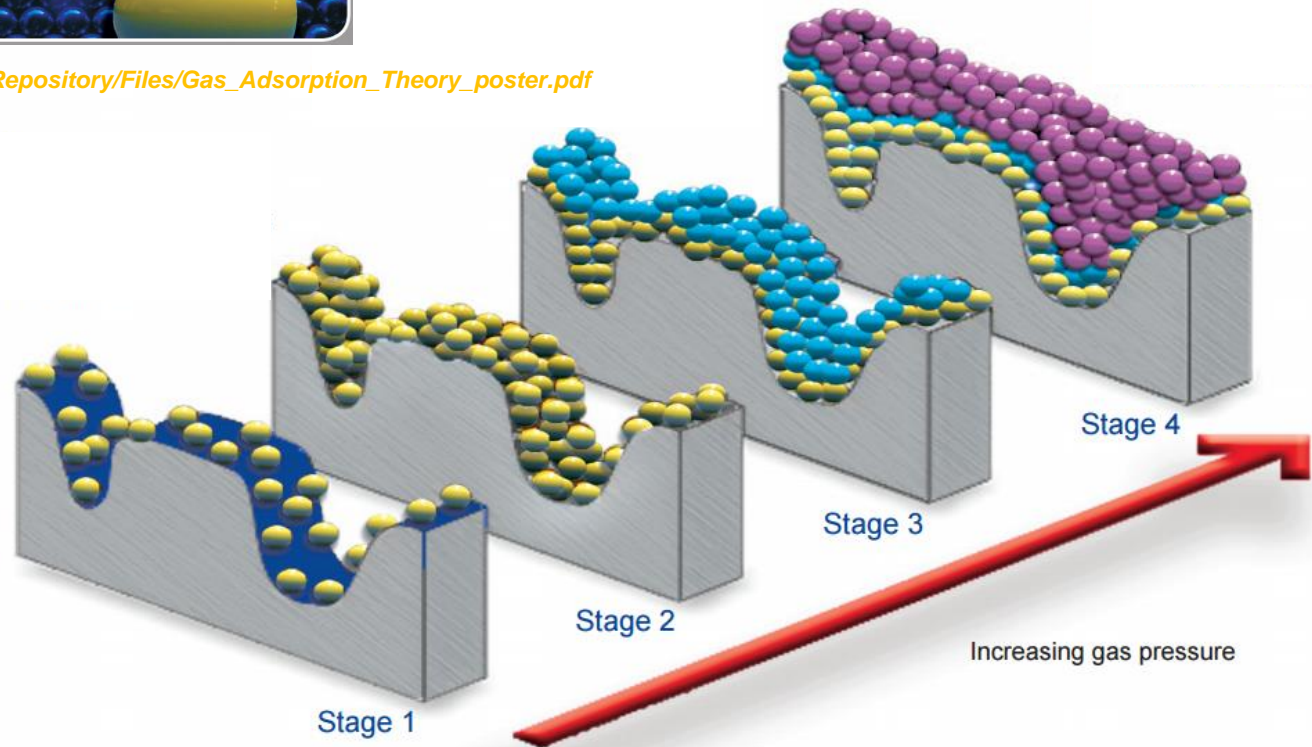
# Introduction



*Grain surface (Adsorbent)*

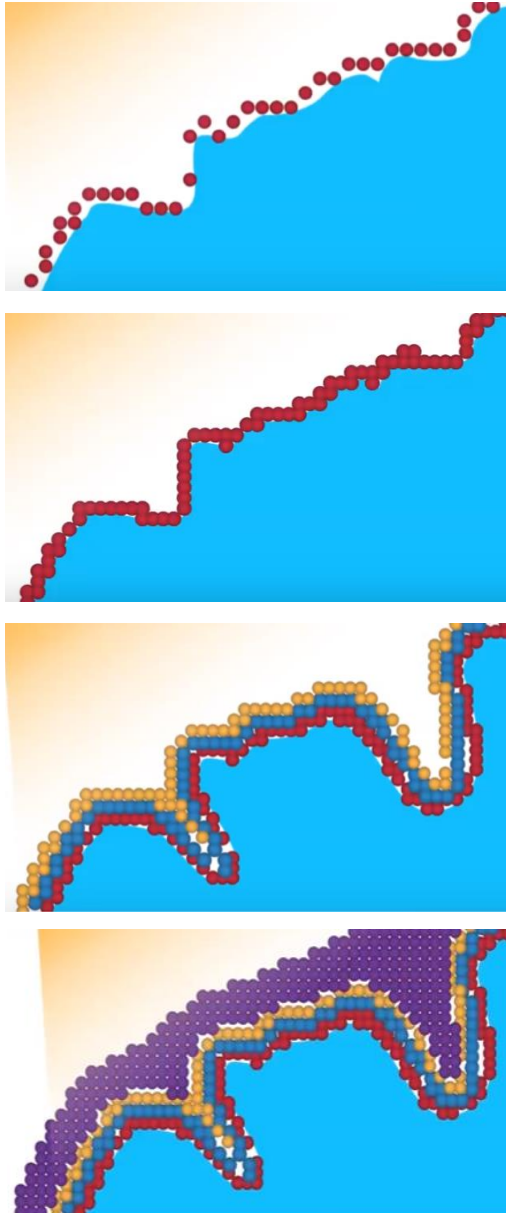
*Nitrogen molecule (Adsorbate)*

[http://www.micromeritics.com/Repository/Files/Gas\\_Adsorption\\_Theory\\_poster.pdf](http://www.micromeritics.com/Repository/Files/Gas_Adsorption_Theory_poster.pdf)

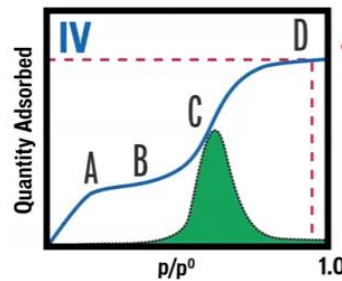
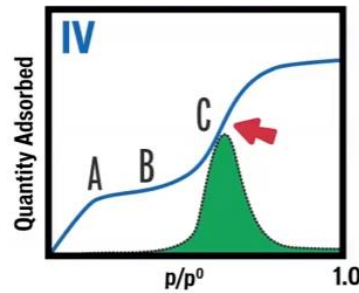
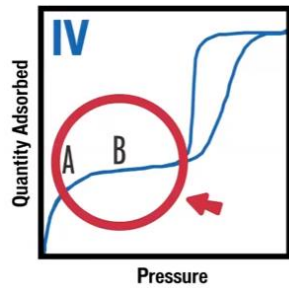
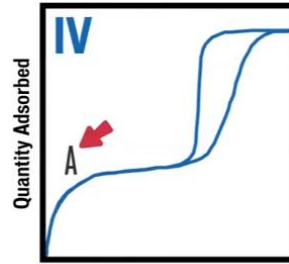


# Introduction

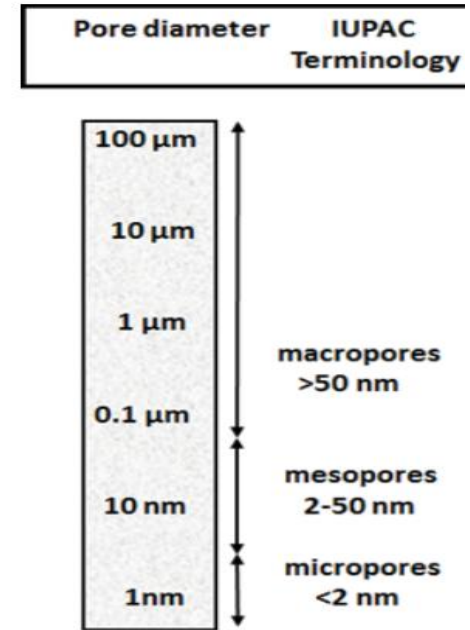
Increasing relative pressure



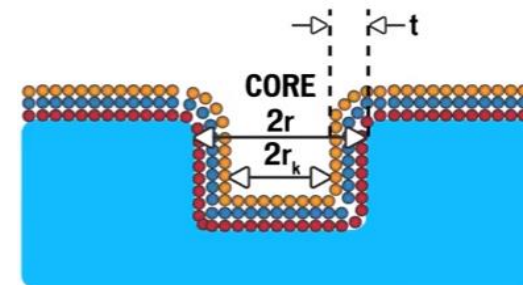
AAPG-ES 2016



University of Oklahoma



<https://www.youtube.com/watch?v=ICh-VtEzNvk>

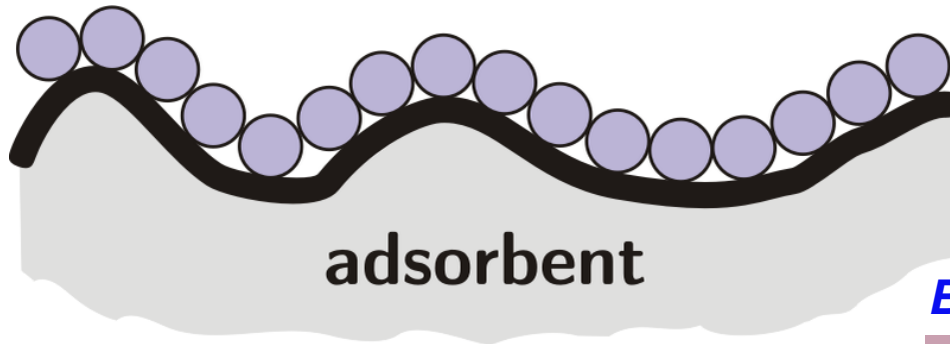


Misra



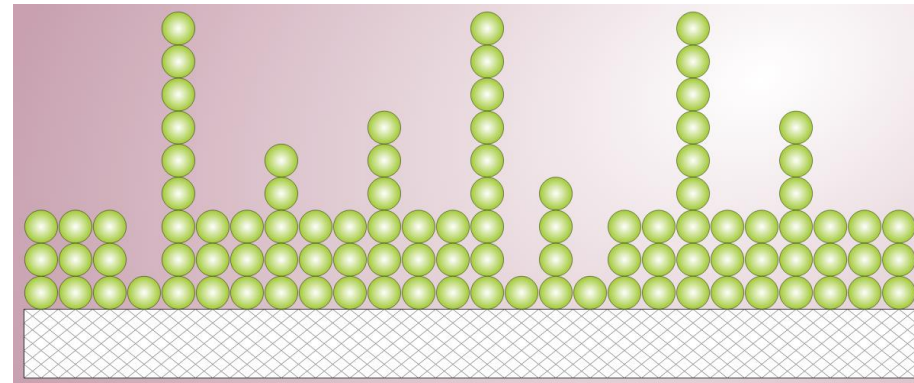
# Introduction: Mono- vs Multi-Layer Adsorption

*Langmuir Equation : Monolayer adsorption*



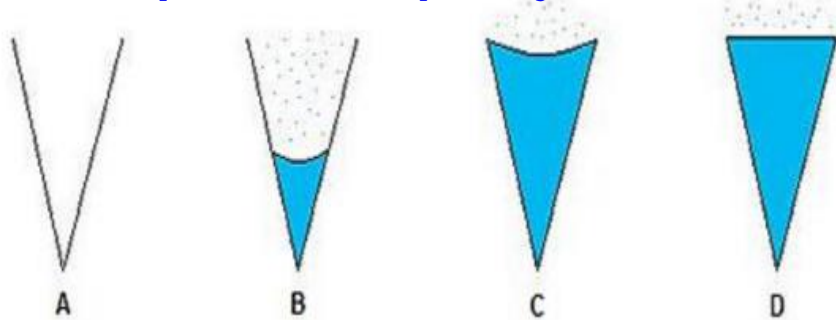
[https://commons.wikimedia.org/wiki/File:Langmuir\\_izoterma.png](https://commons.wikimedia.org/wiki/File:Langmuir_izoterma.png)

*BET Equation : Multi-Layer Adsorption*



[https://en.wikipedia.org/wiki/BET\\_theory#/media/File:BET\\_Multilayer\\_Adsorption.svg](https://en.wikipedia.org/wiki/BET_theory#/media/File:BET_Multilayer_Adsorption.svg)

*Kelvin Equation : Capillary Condensation*

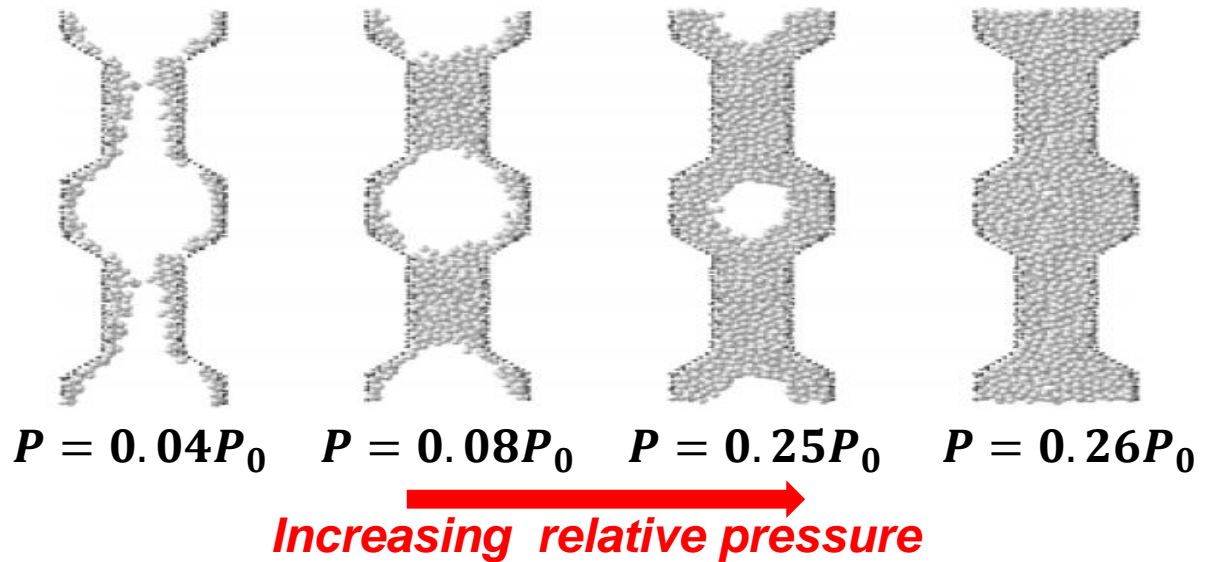


[https://en.wikipedia.org/wiki/Capillary\\_condensation](https://en.wikipedia.org/wiki/Capillary_condensation)

# Introduction: Adsorption vs Desorption

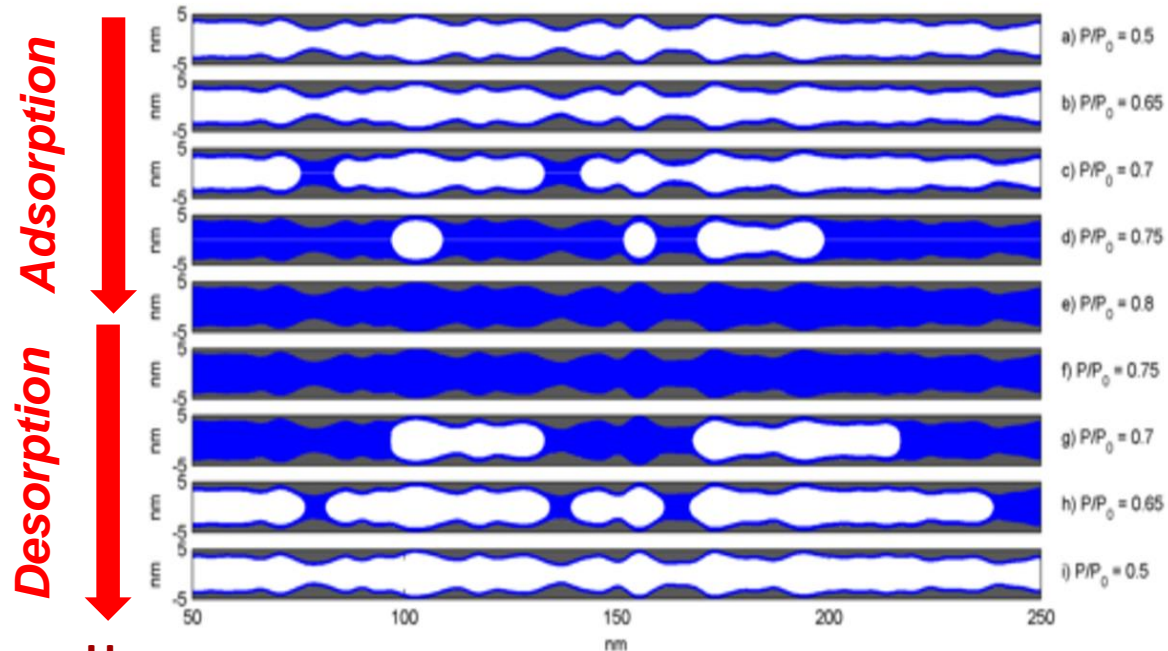
*Adsorption of Argon atoms in 5 nm silica pore with 2.5 nm constriction*

*Coasne et al., 2005*



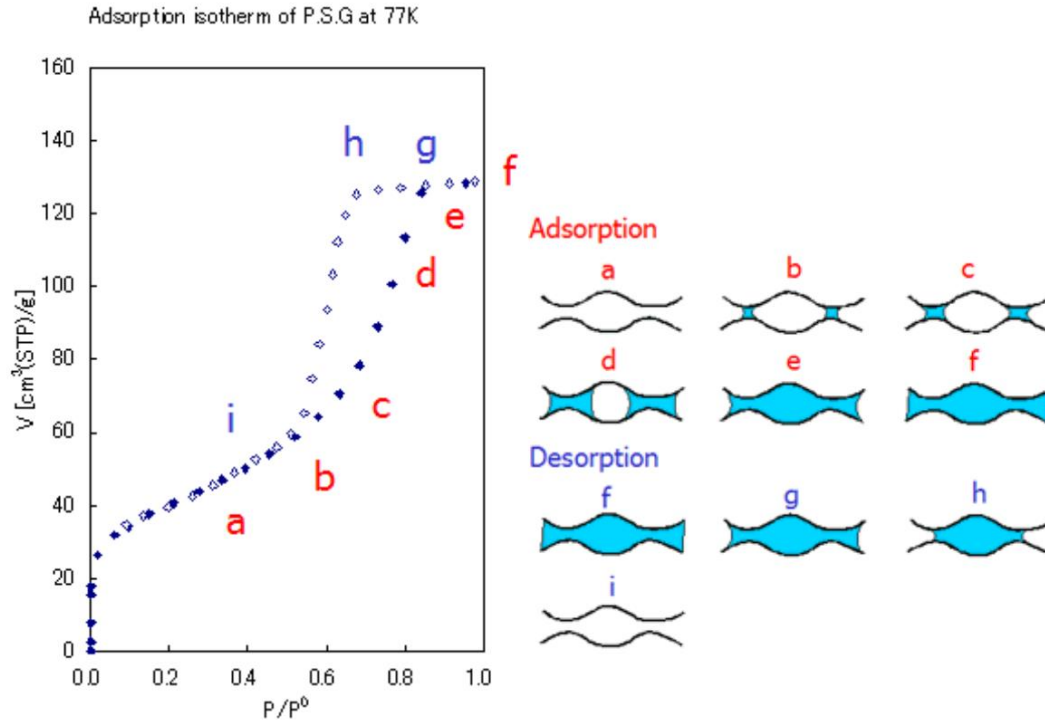
*Configuration of adsorbate in a corrugated mesopore during adsorption and desorption*

<http://www.nce.ulg.ac.be/gommes/research.php>

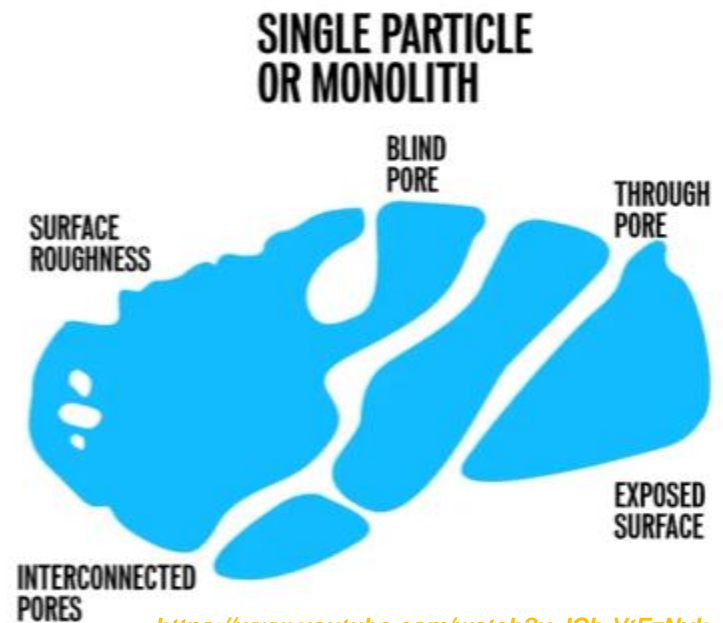




# Introduction: Adsorption vs Desorption

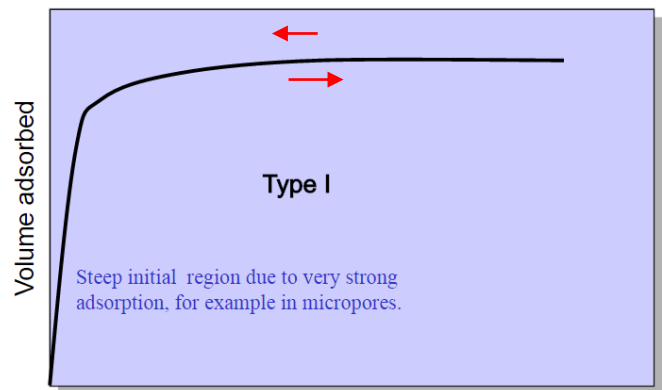


<http://www.microtrac-bel.com/en/tech/bel/seminar16.html>

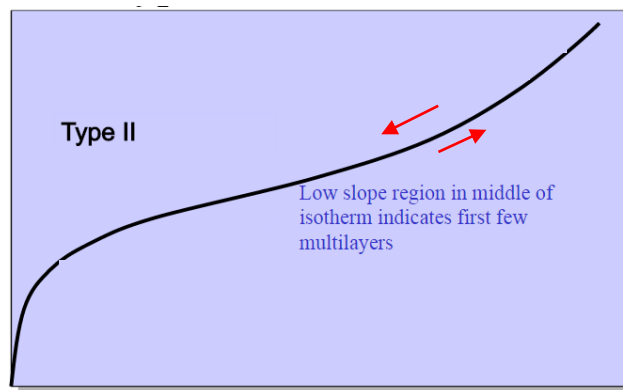


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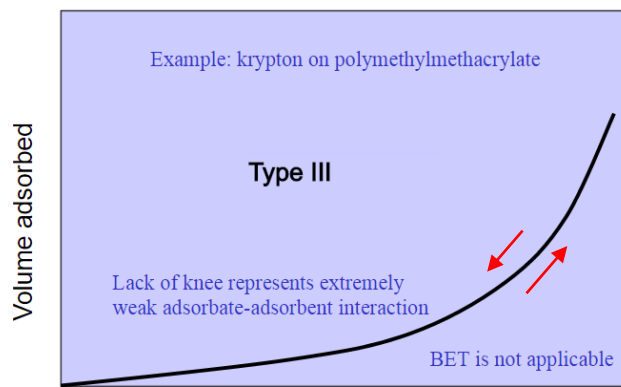
# Introduction: Isotherm Types



Relative Pressure ( $P/P_0$ )

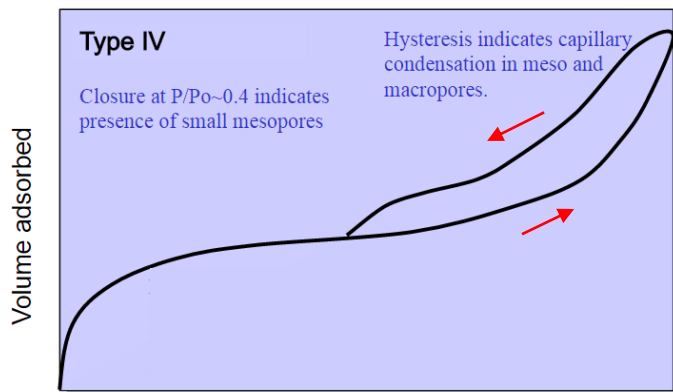


Relative Pressure ( $P/P_0$ )

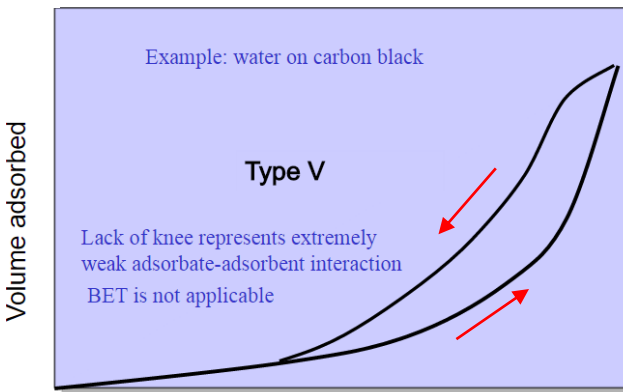


Relative Pressure ( $P/P_0$ )

Quantachrome: <http://slideplayer.com/slide/1710170/>

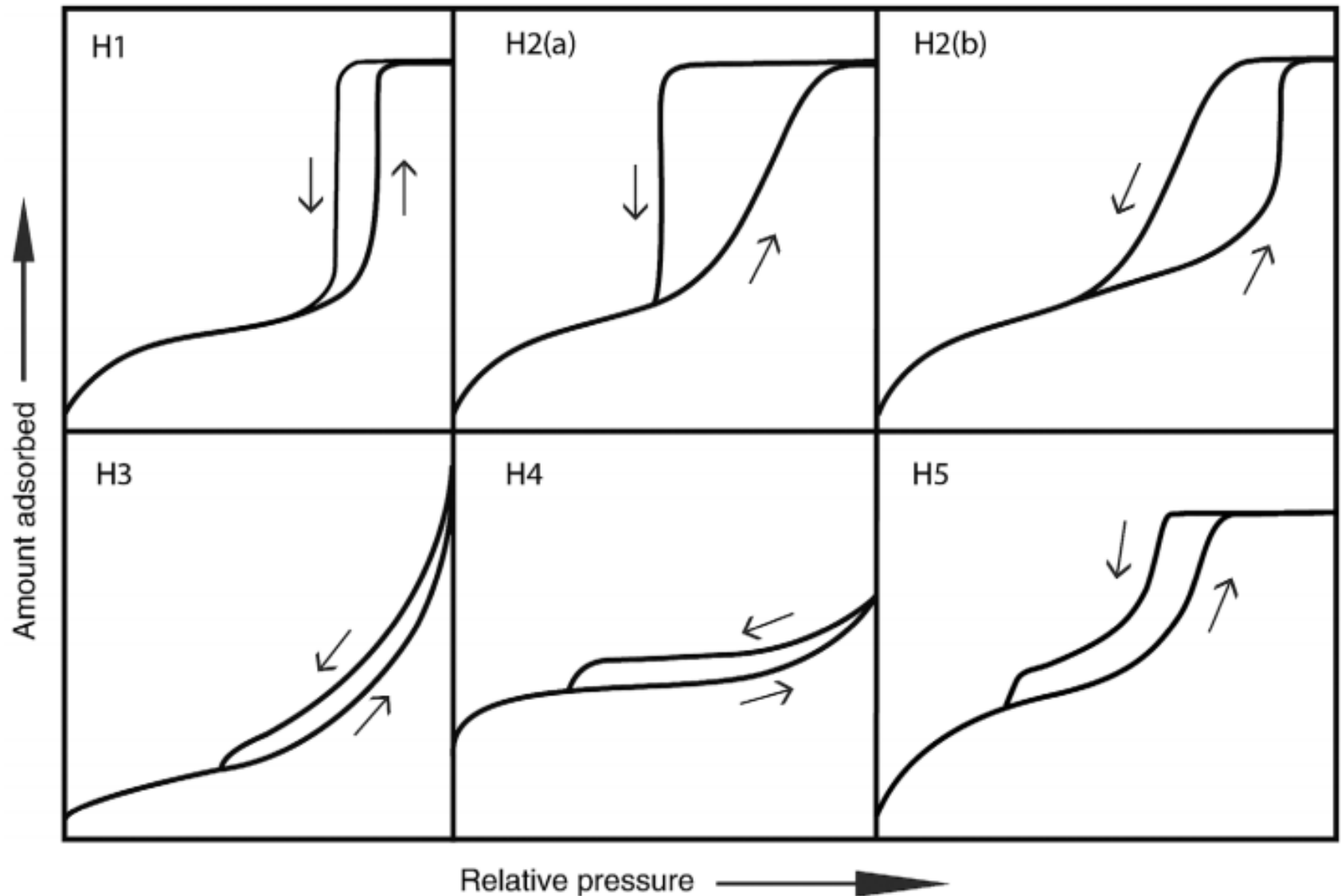


Relative Pressure ( $P/P_0$ )



Relative Pressure ( $P/P_0$ )

# Introduction: Hysteresis Types

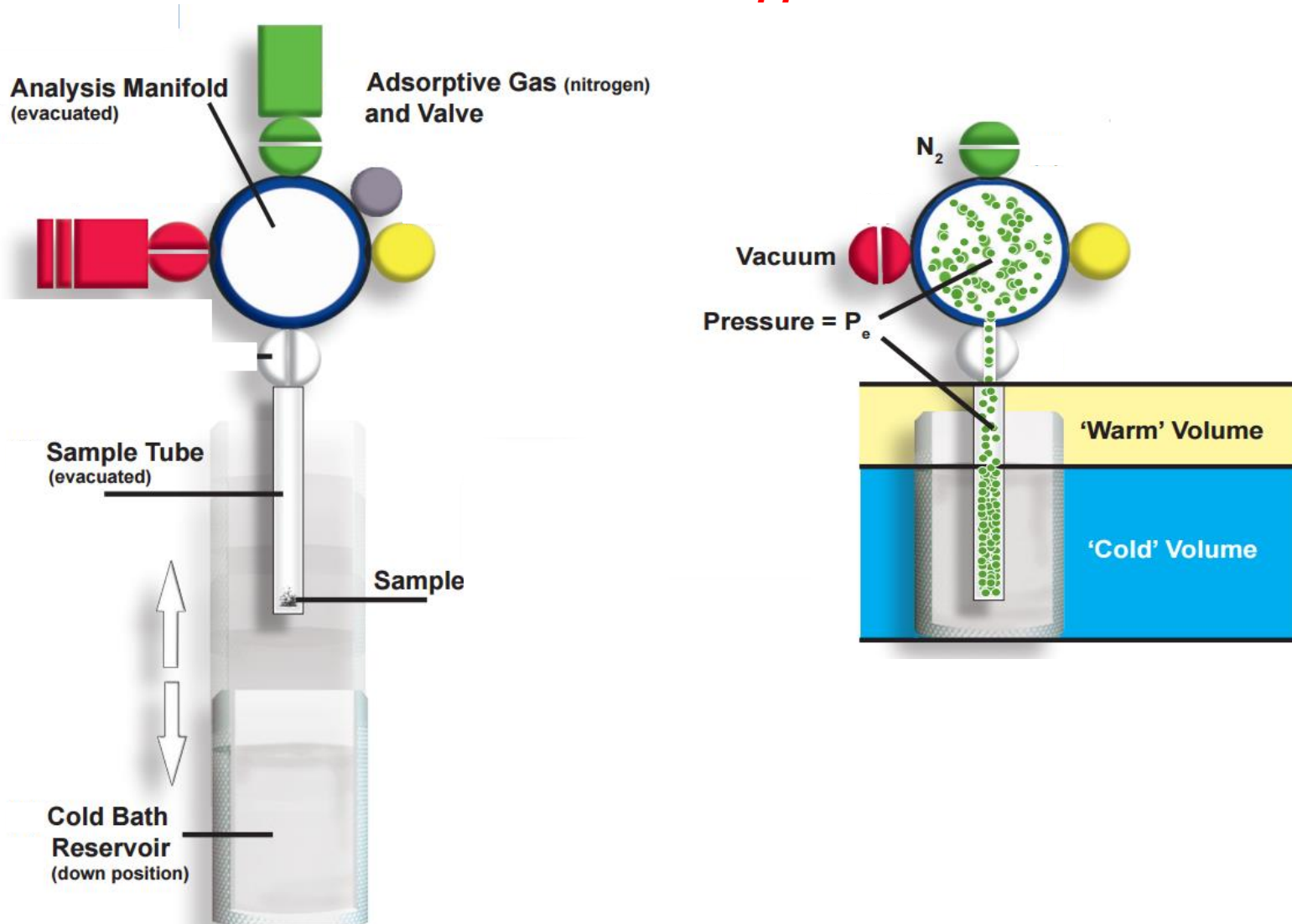


# Motivation

- Identify permeability jail, decline in hydrocarbon production rate, and water production in low-permeability reservoirs
- Currently, there are limited direct/indirect laboratory-based techniques to measure or estimate relative permeability of shales
- Use laboratory adsorption-desorption measurement on shale samples to estimate pore-size distribution, pore connectivity, and relative permeability for pore size in the range of 7 nm to 200 nm
- Compare these estimates across oil , condensate, and gas windows of Eagle Ford shale and Wolfcamp shale
- Investigate the effects of organic matter on these estimates

# Adsorption-Desorption Isotherm Measurements

## *Micromeritics ADI Apparatus*



# Adsorption-Desorption Isotherm Measurements

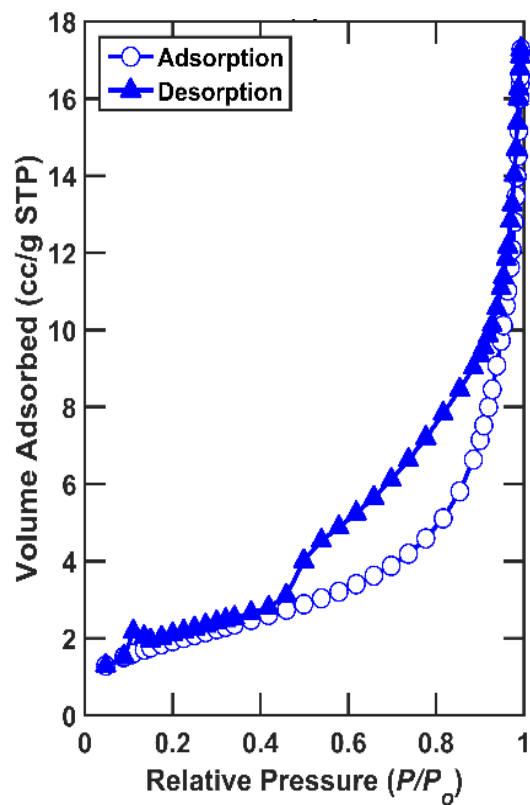
## *Rock Samples*

Formation	Maturity	Number of samples	TOC, wt%	Porosity, %	Clay, wt%	Non-clay, wt%
Wolfcamp	Condensate	8	0.2 – 15.5	4.49 – 11.52	44 – 70	10 – 30
Eagle Ford	Gas	9	0.4 – 3.3	4.27 – 8.33	10 – 20	60 – 80
	Oil	6	1.5 – 4.9	7.65 – 10.22		

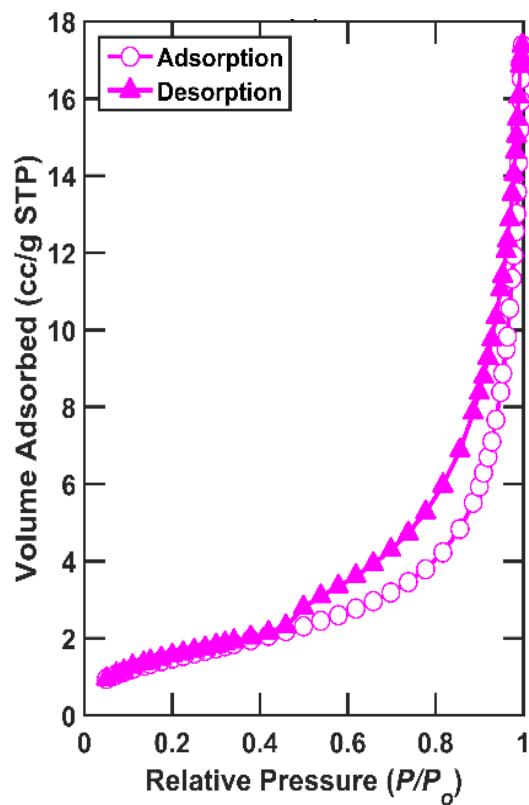


# Adsorption-Desorption Isotherm Measurements

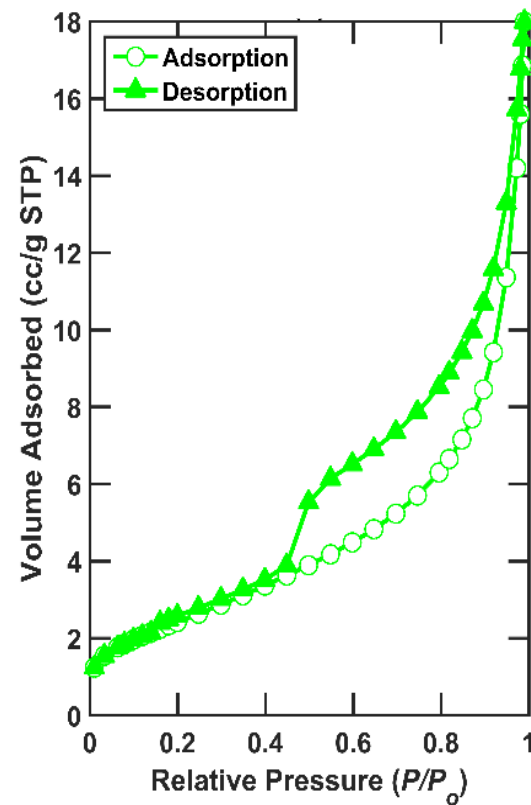
*Comparison across various windows*



*Eagle Ford  
Gas-Window Sample*



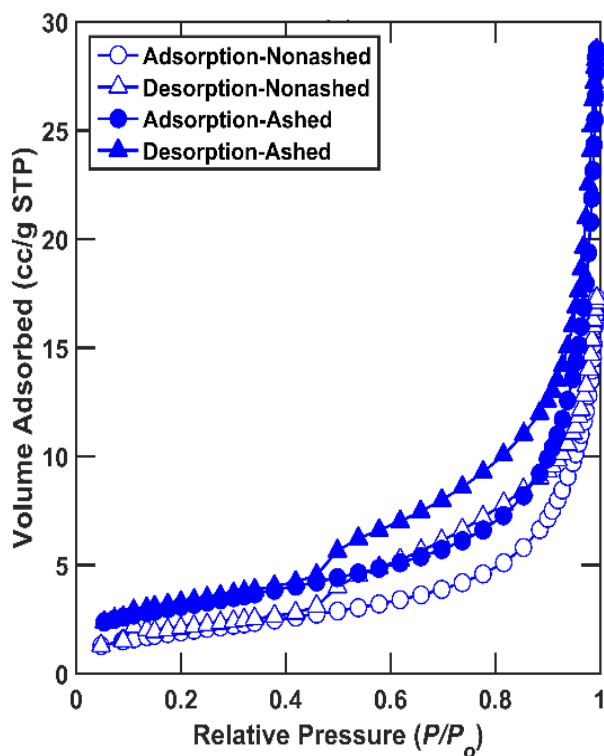
*Eagle Ford  
Oil-Window Sample*



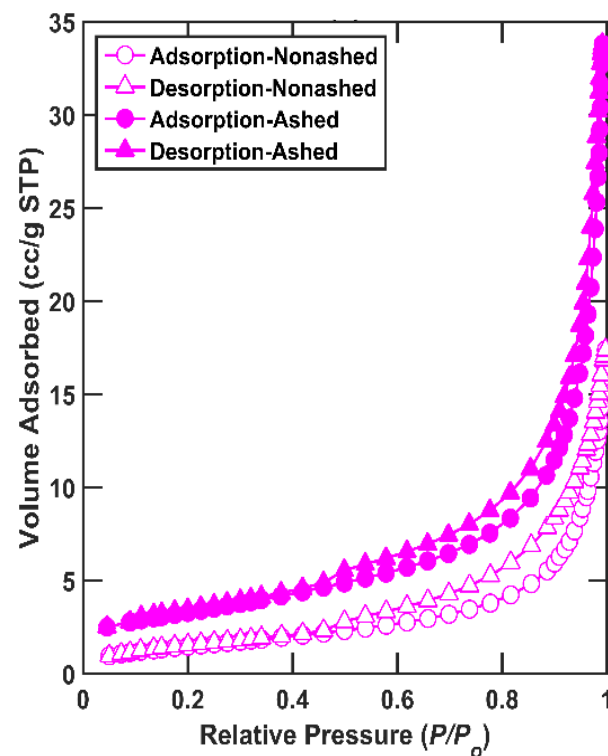
*Wolfcamp Condensate-  
Window Sample*

# Adsorption-Desorption Isotherm Measurements

## *Effect of removal of organic matter*

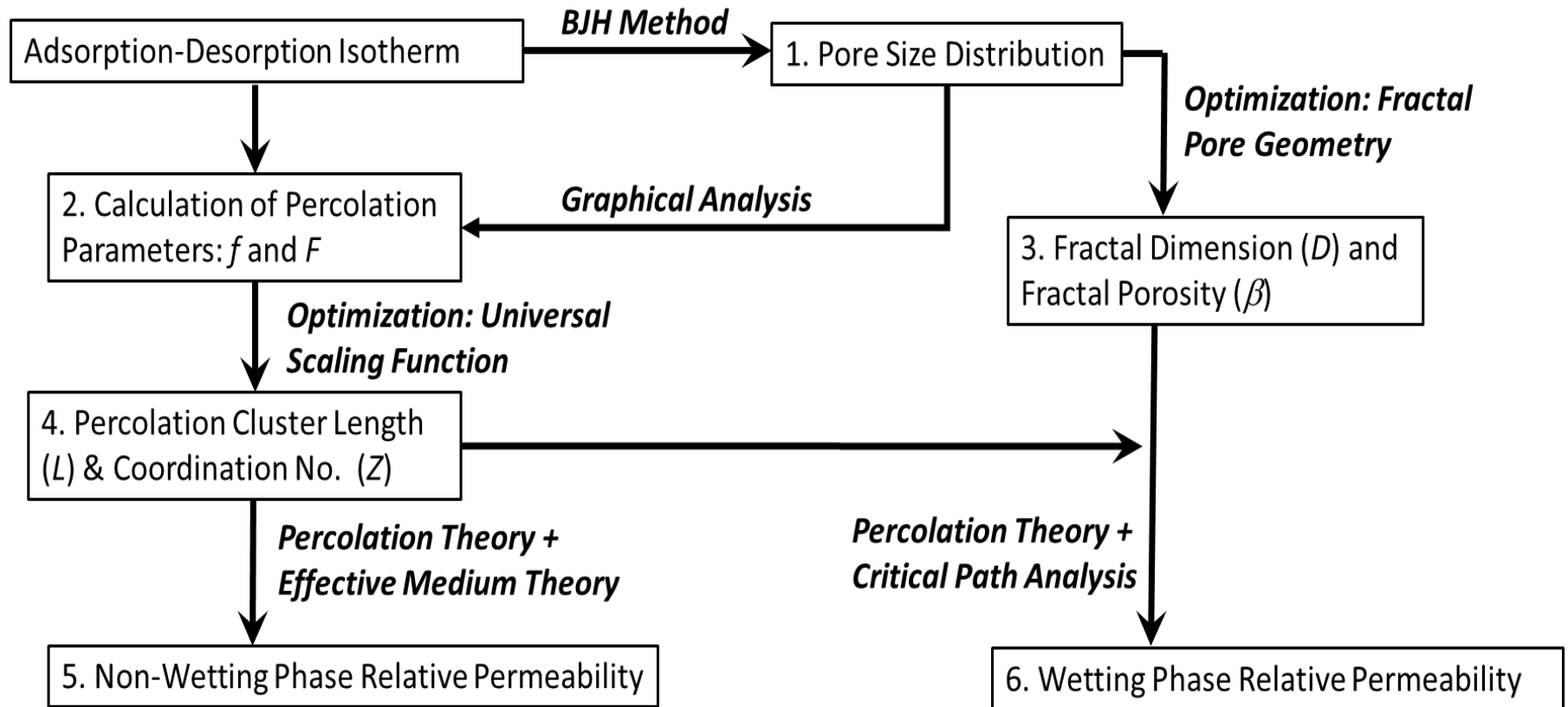


*Eagle Ford  
Gas-Window Sample*



*Eagle Ford  
Oil-Window Sample*

# Interpretation Methodology



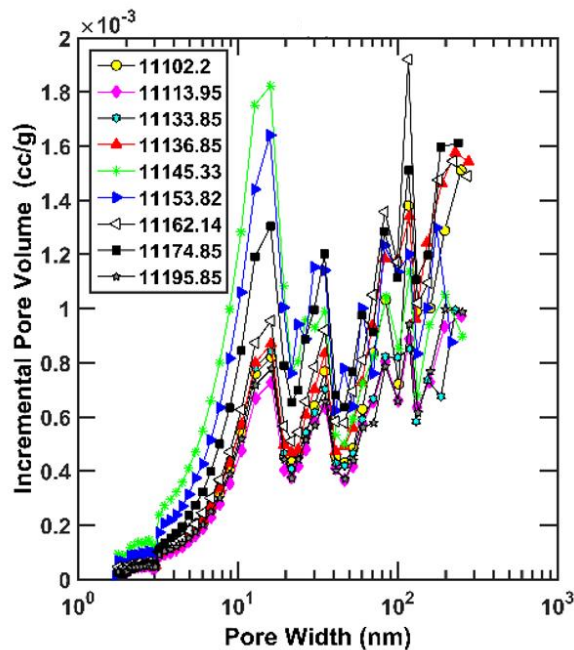
# Results: Pore Size Distribution

*Thickness of adsorbed layer*

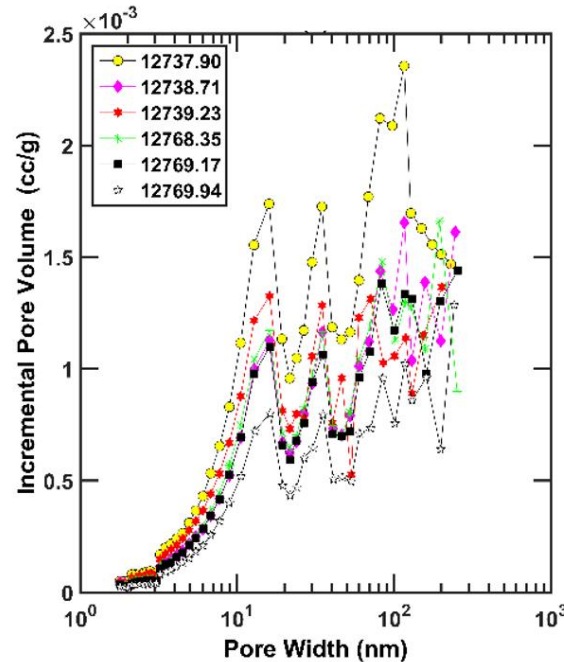
*Pore radius in which condensation occurs*

$$t = 0.1 \left( \frac{60.65}{0.03071 - \log \left( \frac{P}{P_o} \right)} \right)^{0.3968}$$

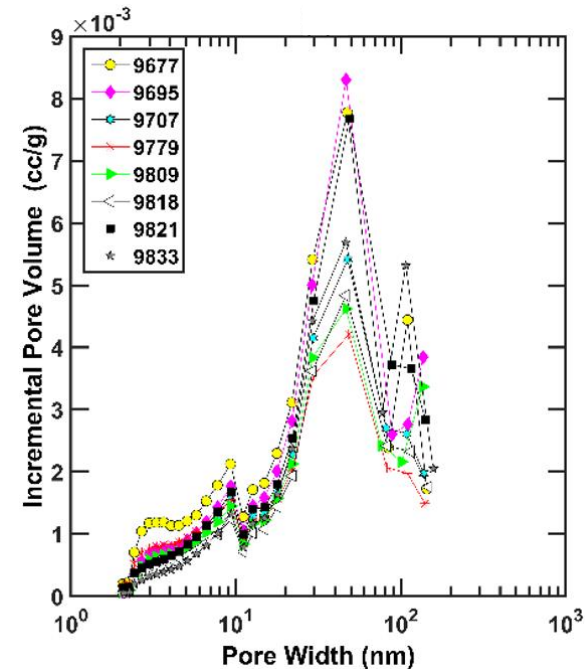
$$r = \left( \frac{2\gamma V_L}{RT \ln \left( \frac{P}{P_o} \right)} \right) + t + 0.3$$



**Eagle Ford  
Gas-Window Sample**



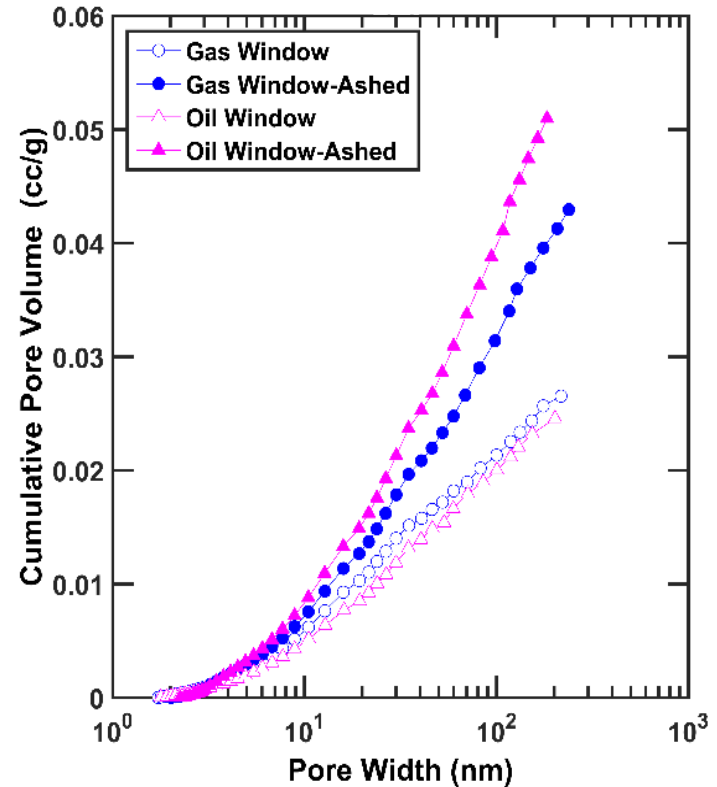
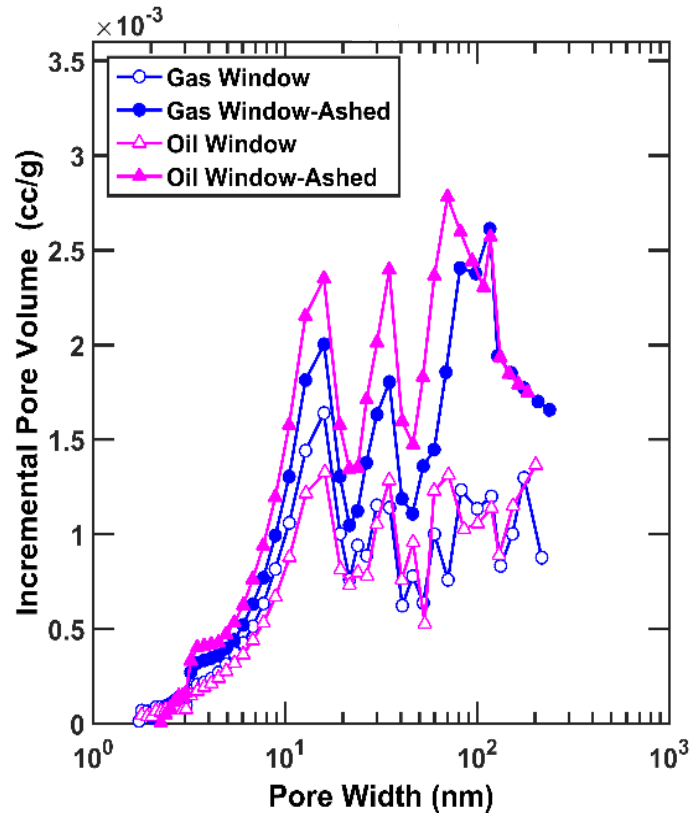
**Eagle Ford  
Oil-Window Sample**



**Wolfcamp Condensate-  
Window Sample**

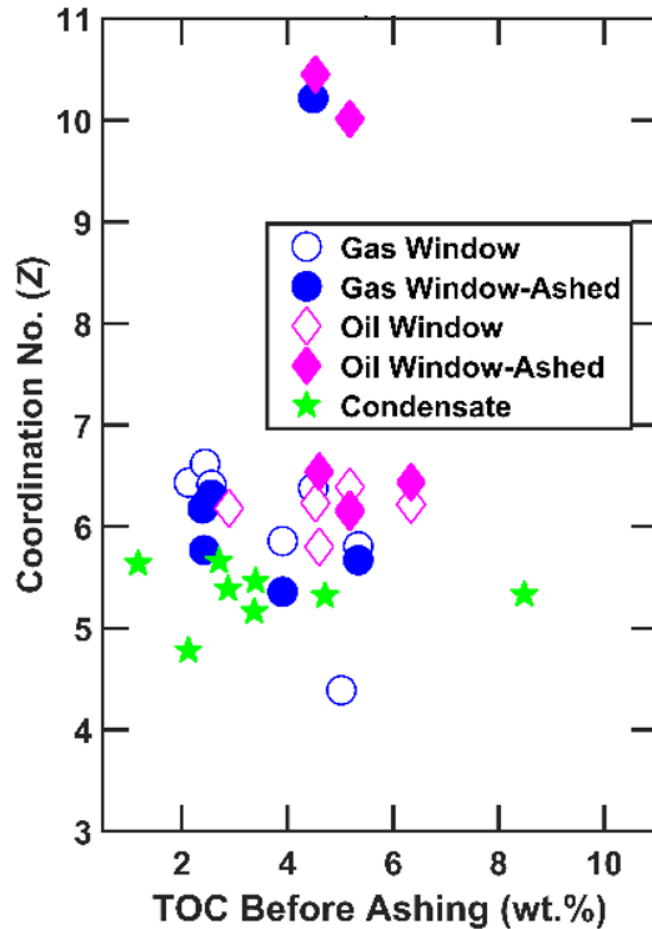
# Results: Pore Size Distribution

## *Effect of removal of organic matter*

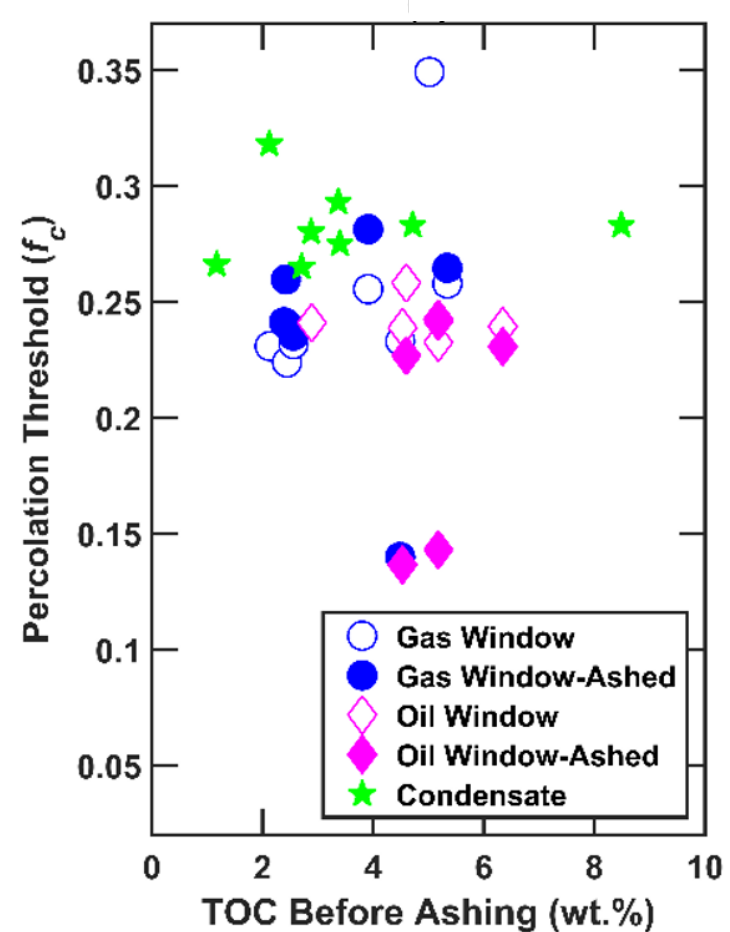


*Eagle Ford Samples*

# Results: Pore Connectivity



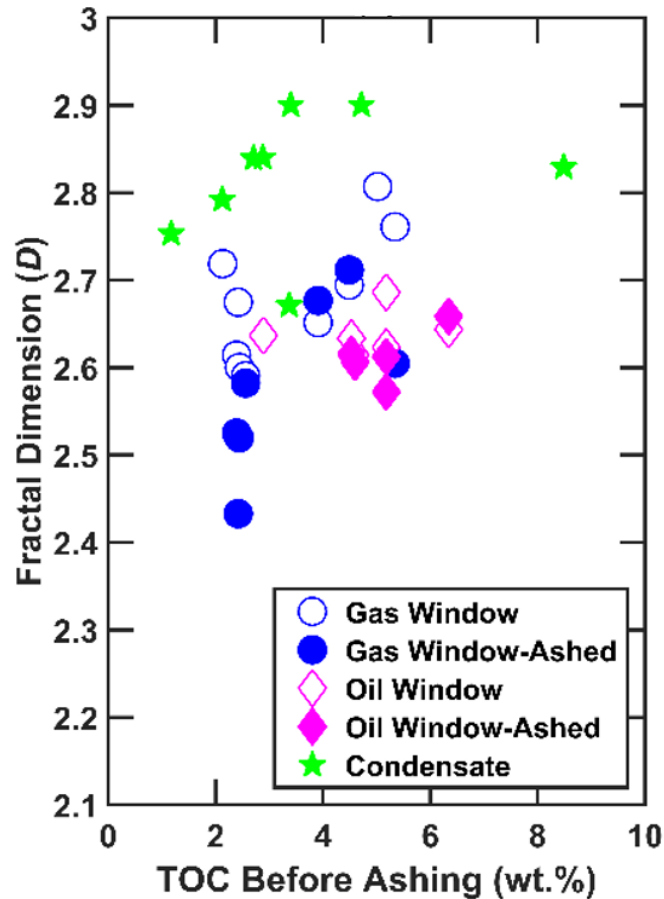
*Short-Range  
Pore Connectivity*



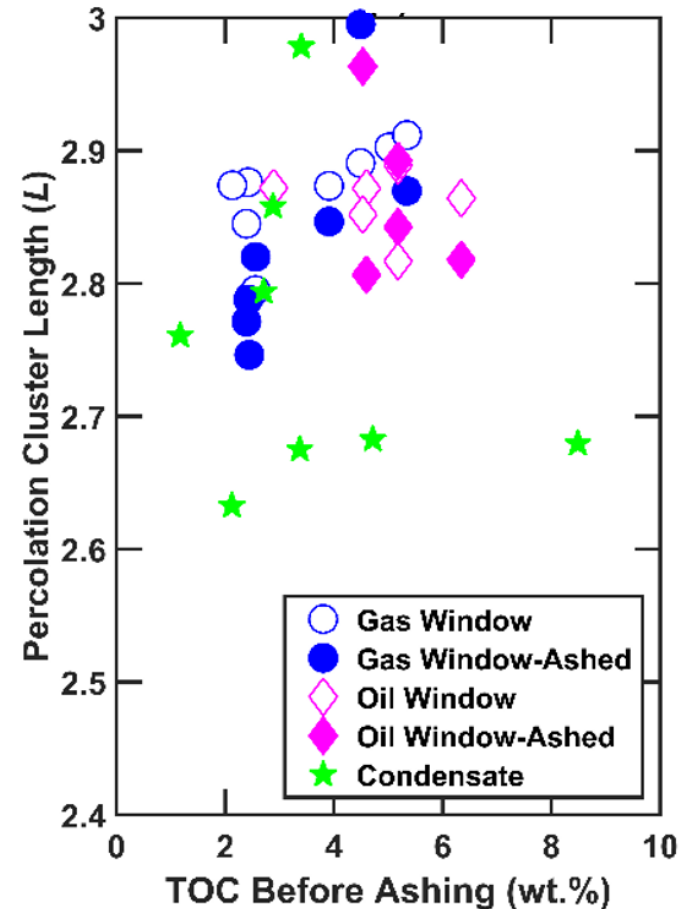
*Long-Range  
Pore Connectivity*



# Results: Pore Complexity

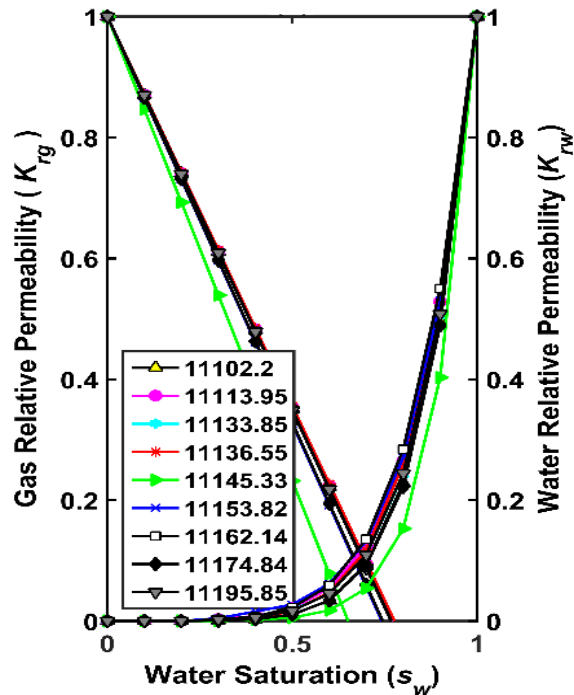


*Pore Complexity*

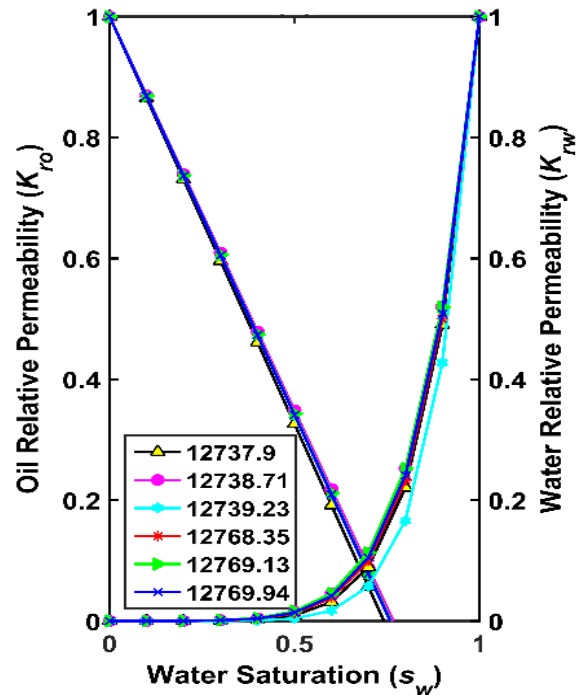


*Dead end vs connected pores*

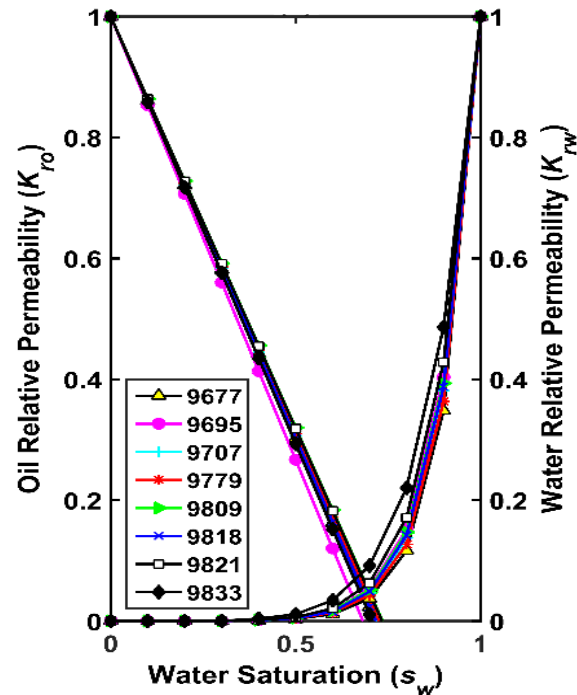
# Results: Relative Permeability



*Eagle Ford  
Gas-Window Sample*

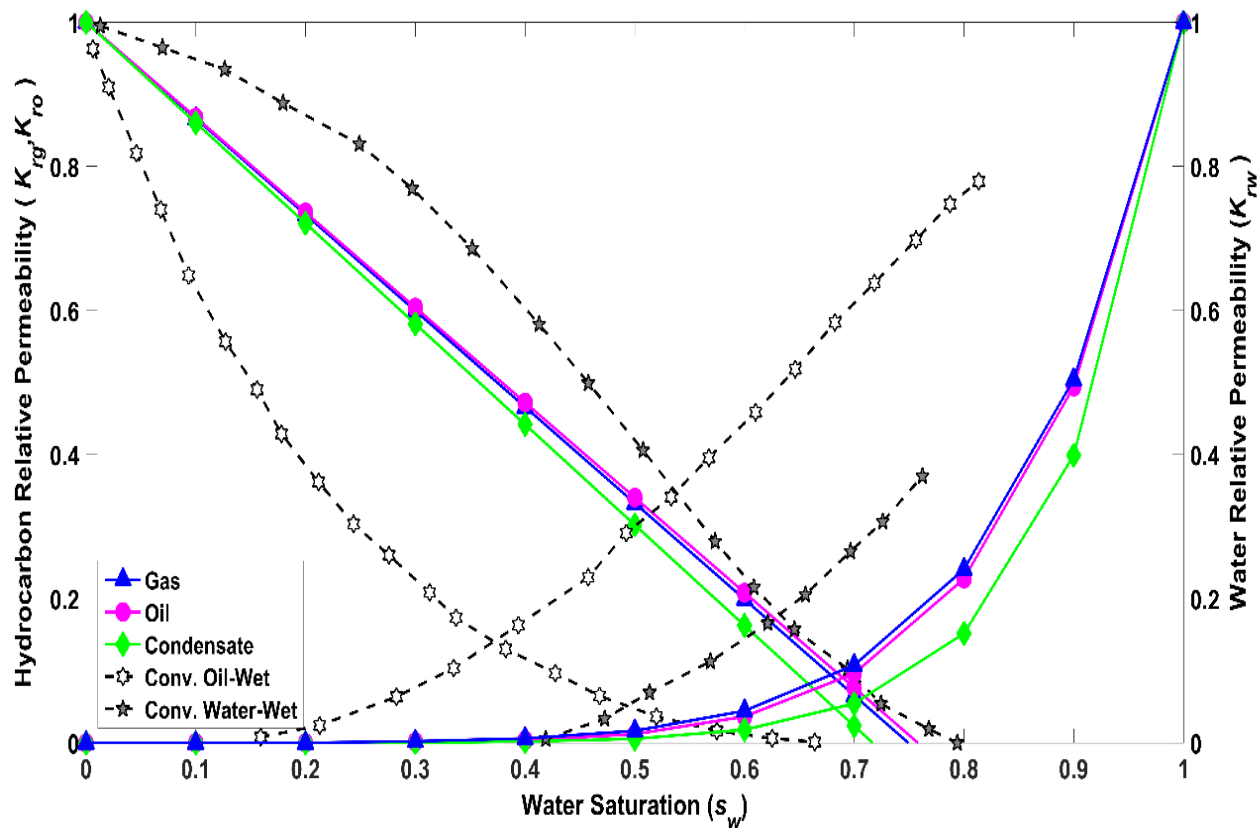


*Eagle Ford  
Oil-Window Sample*



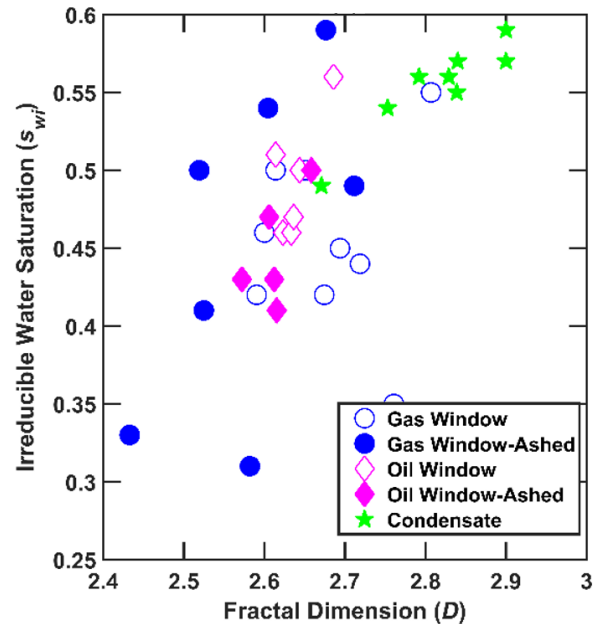
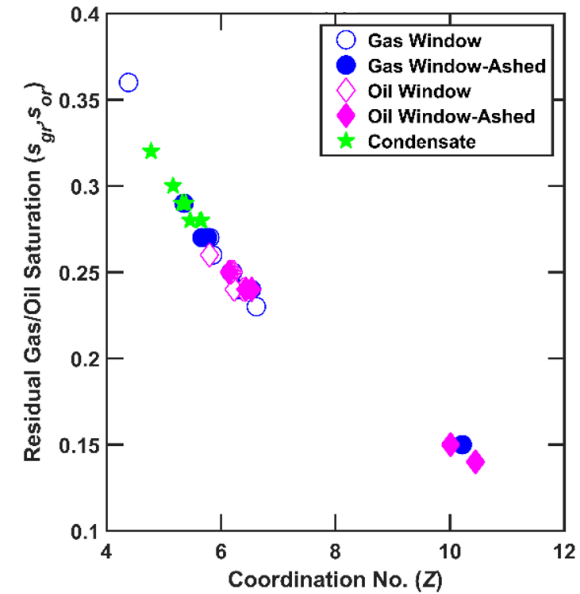
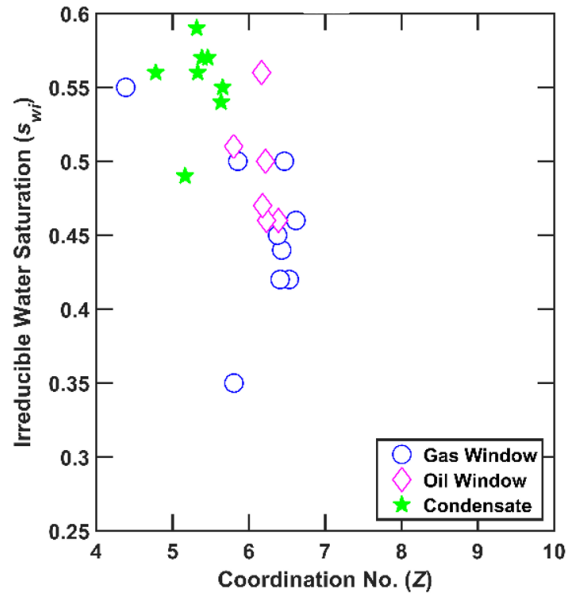
*Wolfcamp Condensate-  
Window Sample*

# Results: Relative Permeability



	Non-Ashed			Ashed	
	Eagle Ford Gas	Eagle Ford Oil	Wolfcamp Condensate	Eagle Ford Gas	Eagle Ford Oil
$s_{gr} / s_{or}$	0.23-0.36	0.24-0.26	0.28-0.32	0.15-0.29	0.14-0.26
$s_{wi}$	0.35-0.55	0.46-0.56	0.49-0.59	0.31-0.59	0.41-0.5

# Results: Residual Saturations



- Relative permeability curves exhibit minimal variation with depth
- Samples exhibit large variations in kerogen content, pore connectivity, range of connected pore network, pore complexity, and saturations
- Relative permeability estimates support the low water-cut during hydrocarbon production, absence of correlation between hydrocarbon production decline and increase in water production, and existence of permeability jail in shale formations
- Our interpretation methodology indicates that Eagle Ford samples will have better flow capacity compared to Wolfcamp samples

**Thank You**