

Use of a Dual-Continuum Approach for Modeling Coupled Hydro-mechanical Processes of CO₂ Injection at In Salah, Algeria*

Hui-Hai Liu¹ and Jonny Rutqvist¹

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¹Lawrence Berkeley National Laboratory, Berkeley, CA (hhliu@lbl.gov)

Descriptive Statement

Presented here is a newly developed dual-continuum approach for modeling coupled hydro-mechanical processes and its application in studying CO₂ injection at In Salah site in Algeria.

References

Coyner, K.B., 1984, Effects of Stress, Pore Pressure, and Pore Fluids on Bulk Strain, Velocity, and Permeability of Rocks, Ph.D. Dissertation, Massachusetts Institute of Technology.

Iding, M. and P. Ringrose, 2010, Evaluating the impact of fractures on the performance of the In Salah CO₂ storage site: International Journal of Greenhouse Gas control, v. 4/2, p. 242-248.

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Website

Wright, I., 2006, CO₂ Geological Storage: Two Years Operation at In Salah (Algeria): Website accessed 17 September 2008.
http://www.co2management.org/proceedings/CO2_Geological_Storage_Two_Years_Operation_in_Algeria_Ian_Wright.pdf

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Earth Sciences Division

Lawrence Berkeley National Laboratory

Berkeley, California

Outline

- A dual-continuum approach for coupled hydro-mechanical processes

A new stress-strain relationship

Governing equations

Effective parameters

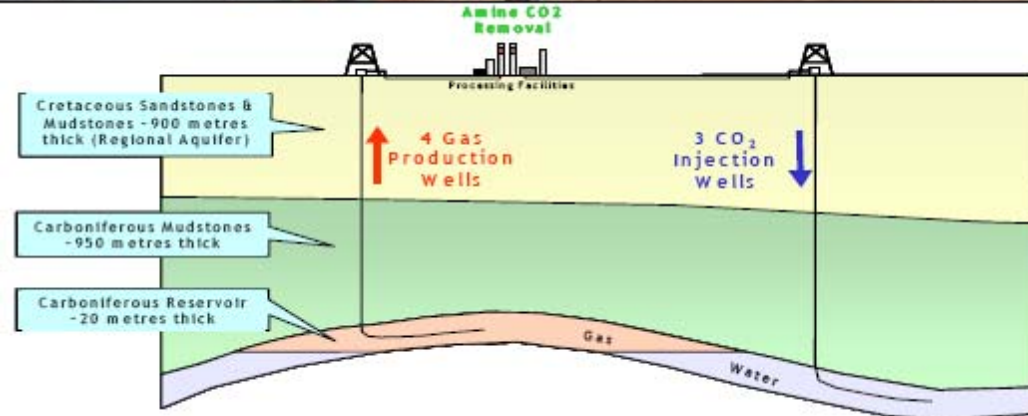
- Simulation of injection at In Salah

Model development

Data use

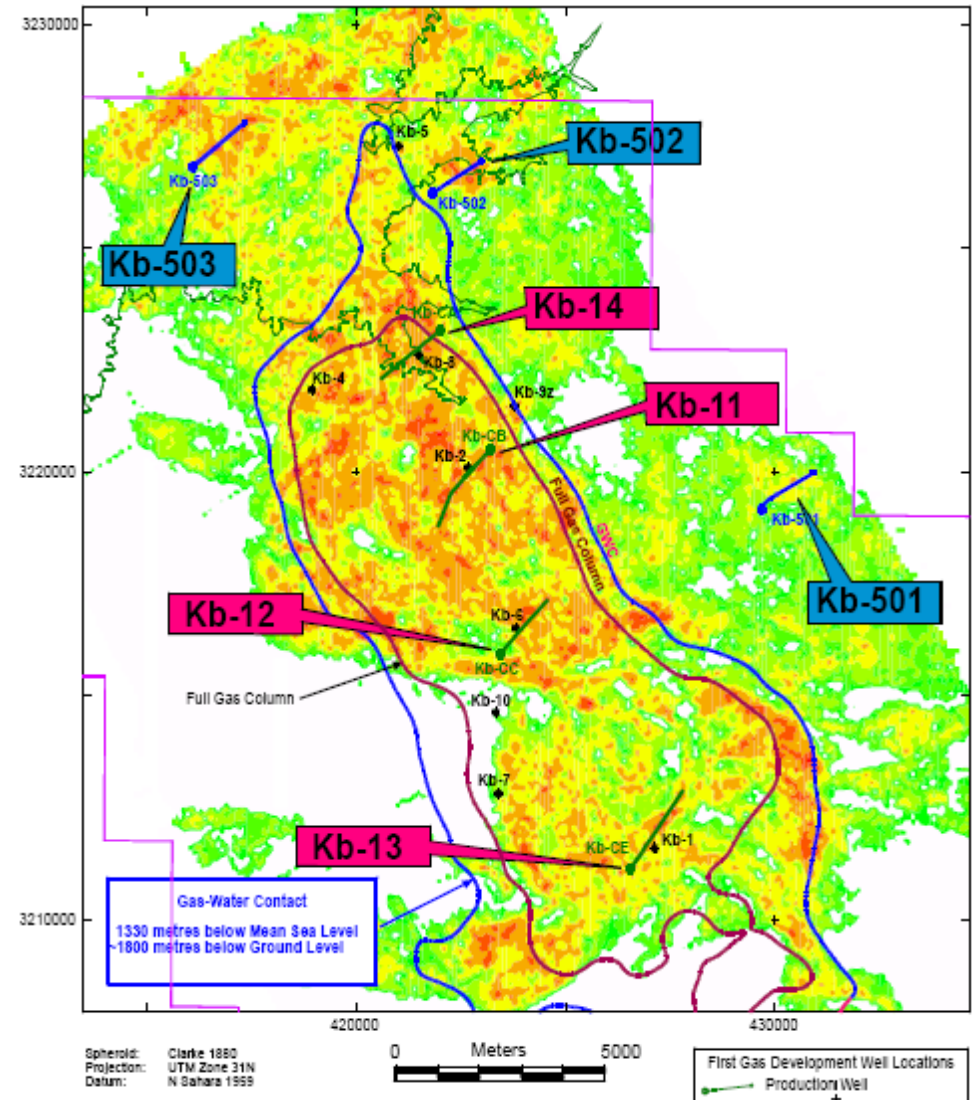
Sensitivity study

CO₂ Geological Sequestration at In Salah



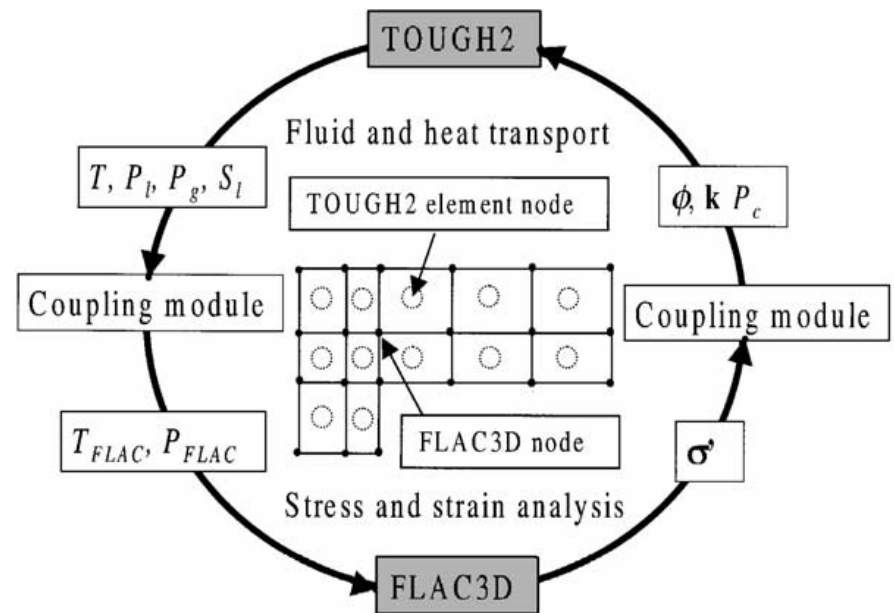
Modified from Wright (2008)

Fractures occur in nearly all geological settings and play a major role for hydrocarbon migration as well as entrapment (Iding and Ringrose, 2008).



Modeling Coupled Hydro-Mechanical Processes Using a Dual-Continuum Approach

- “Fully” and “partially” coupled modeling approaches for hydro-mechanical processes.
- Are governing equations for fluid flow in TOUGH2 (or other reservoir simulators) adequate for deformable rocks?
- How are effective parameters determined for modeling mechanical deformation of a dual-continuum system?



Rutqvist et al. (2002)

A New Stress-Strain Relationship: Theory

- Hooke's Law:

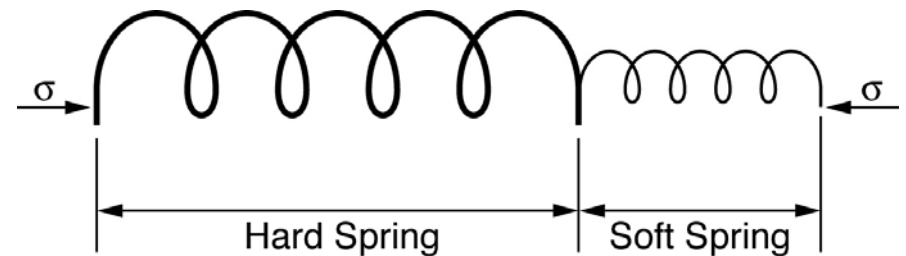
$$d\sigma = Kd\varepsilon_v$$

- Engineering and true (natural) strains

$$d\varepsilon_{v,e} = -\frac{dV}{V_0} \quad d\varepsilon_{v,t} = -\frac{dV}{V}$$

- “Two-Parts” model:

A rock body can be divided into two parts: the hard part and soft part (that corresponds to a fraction of pore volume subject to a large degree of relative deformation [such as cracks])



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•**Stress-Strain Relationship (Liu et al. 2009)**

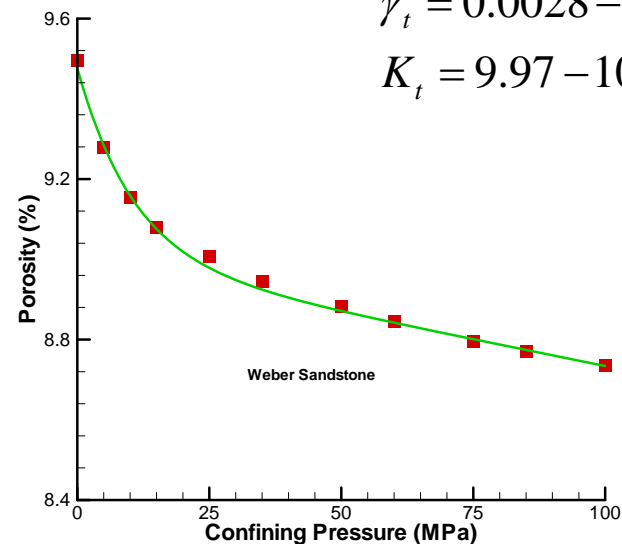
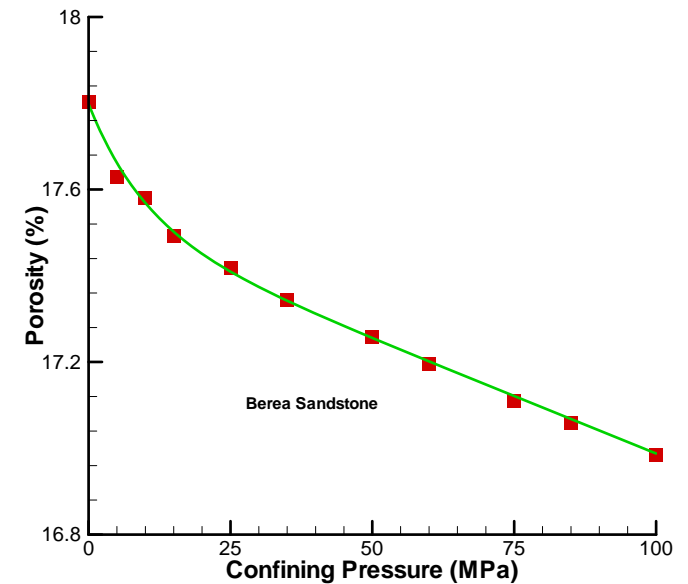
$$-\frac{dV}{V_0} = \gamma_e \frac{d\sigma}{K_e} + \gamma_t \frac{d\sigma}{K_t} \exp\left(-\frac{\sigma}{K_t}\right)$$

A New Stress-Strain Relationship: Rock Porosity

- The derived relationship

$$\phi = \phi_e (1 - C \sigma) + \gamma_t \exp\left(-\frac{\sigma}{K_{t,m}}\right)$$

- The result matches porosity data set (Coyner, 1984)



$$\gamma_t = 0.0028 - 0.0048$$

$$K_t = 9.97 - 10.60 \text{ MPa}$$

A New Stress-Strain Relationship:

Fracture Aperture

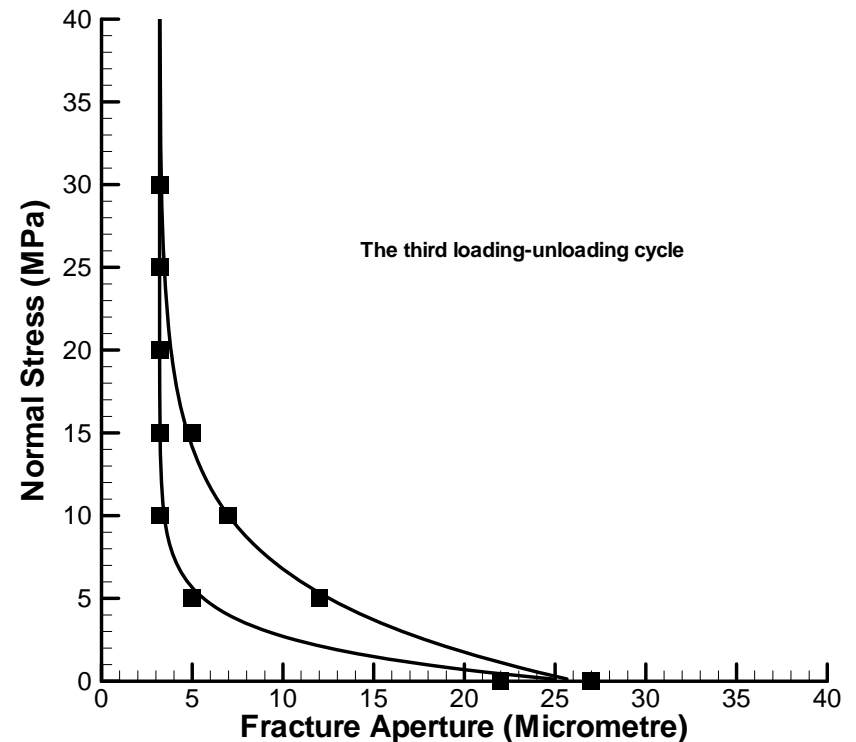
- The derived relationship

$$b = b_{0,e} \left(1 - \frac{\sigma}{K_{F,e}}\right) + b_{0,t} \exp\left(-\frac{\sigma}{K_{F,t}}\right)$$

- The result is consistent with data and an empirical relation (Rutqvist et al., 2002)

$$b \approx b_{0,e} + b_{0,t} \exp\left(-\frac{\sigma}{K_{F,t}}\right)$$

- A significant portion of fracture aperture is “soft”.



A Dual-Continuum Approach: Governing Equations

- Pore Space Conservation

$$\frac{\partial \phi_j}{\partial t} + \nabla \cdot (\phi_j \mathbf{V}_s) = \Phi_j \alpha_j \frac{\partial \varepsilon_{v,j}}{\partial t}$$

- Governing Equation

$$\frac{\partial (M_{j,\psi}^k)}{\partial t} + \nabla \cdot \mathbf{q}_{j,r\psi}^k + \frac{M_{j,\psi}^k}{\phi_j} \left(\Phi_j \alpha_j \frac{\partial \varepsilon_{v,j}}{\partial t} - \frac{\partial \phi_j}{\partial t} \right) - \mathbf{Q}_{j,\psi}^k = 0$$

Additional storage term

A Dual-Continuum Approach: Effective Mechanical Parameters

- Effective stress for a single continuum

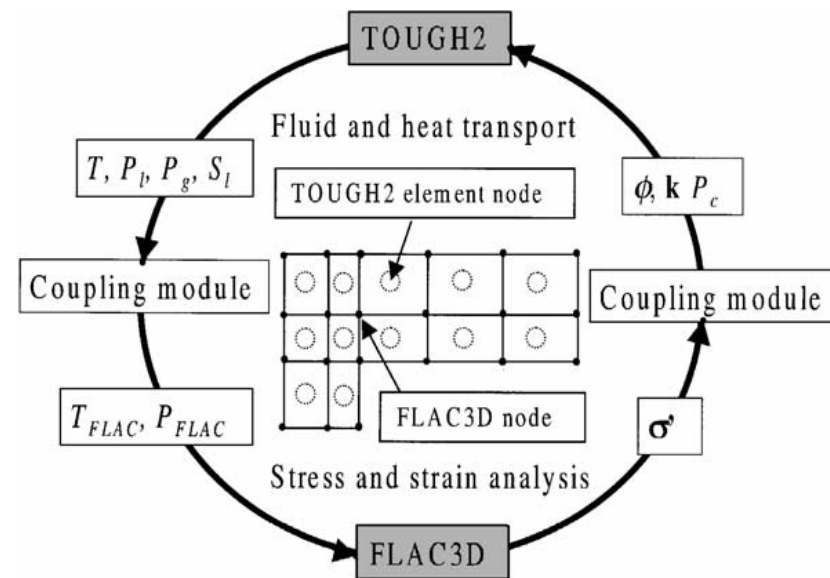
$$\sigma = \sigma_t - \alpha P$$

- Effective stress for a dual-continuum system

$$\sigma = \sigma_t - \frac{\alpha_F \Phi_F K_{eff}}{K_F} P_F - \frac{\alpha_M \Phi_M K_{eff}}{K_M} P_M$$

- Effective modulus for a dual-continuum system

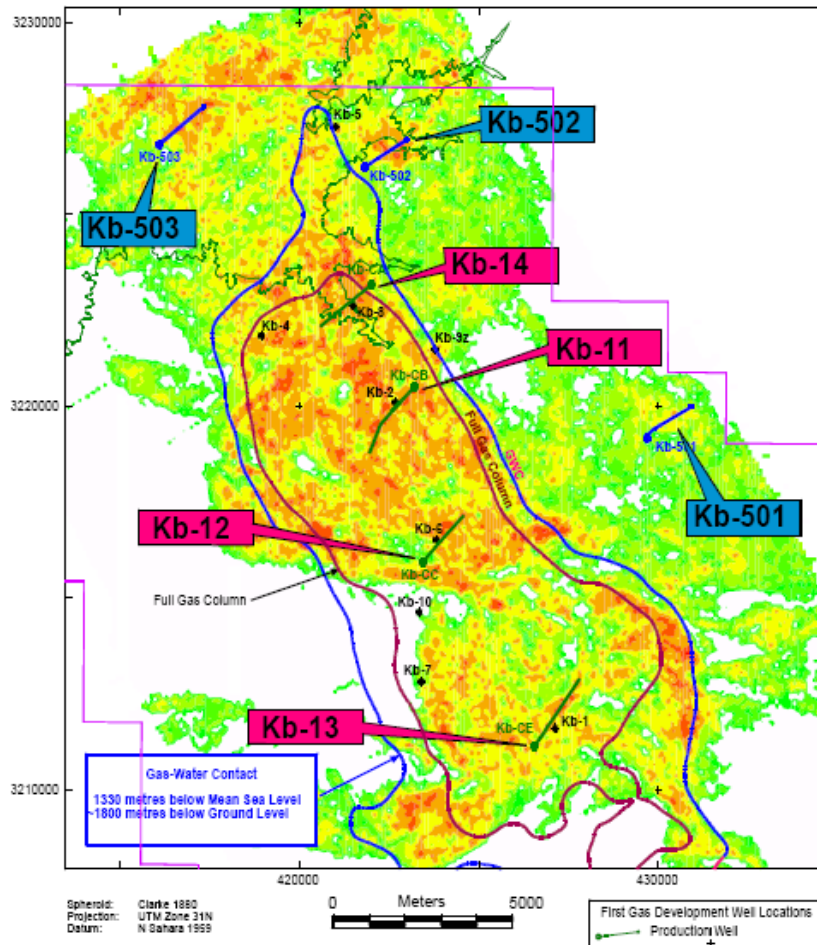
$$K_{eff} = \frac{1}{\frac{\Phi_F}{K_F} + \frac{\Phi_M}{K_M}} \quad K_j = \frac{1}{\frac{\gamma_{e,j}}{K_{e,j}} + \frac{\gamma_{t,j}}{K_{t,j}} \exp\left(-\frac{\sigma_j}{K_{t,j}}\right)}$$



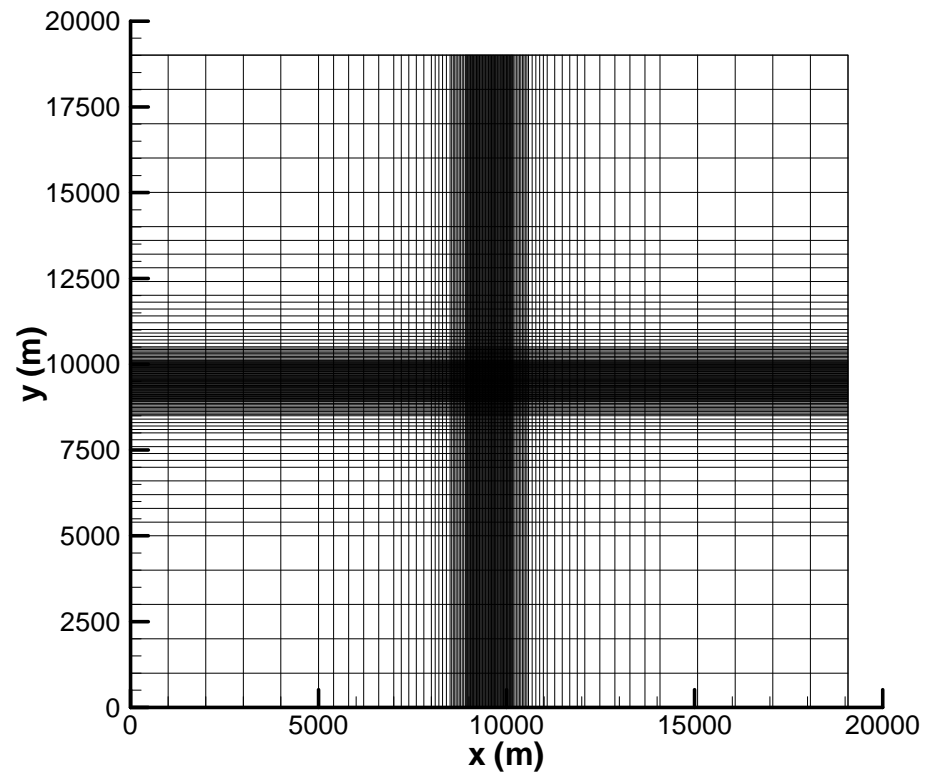
Rutqvist et al. (2002)

Simulation of injection at In Salah:

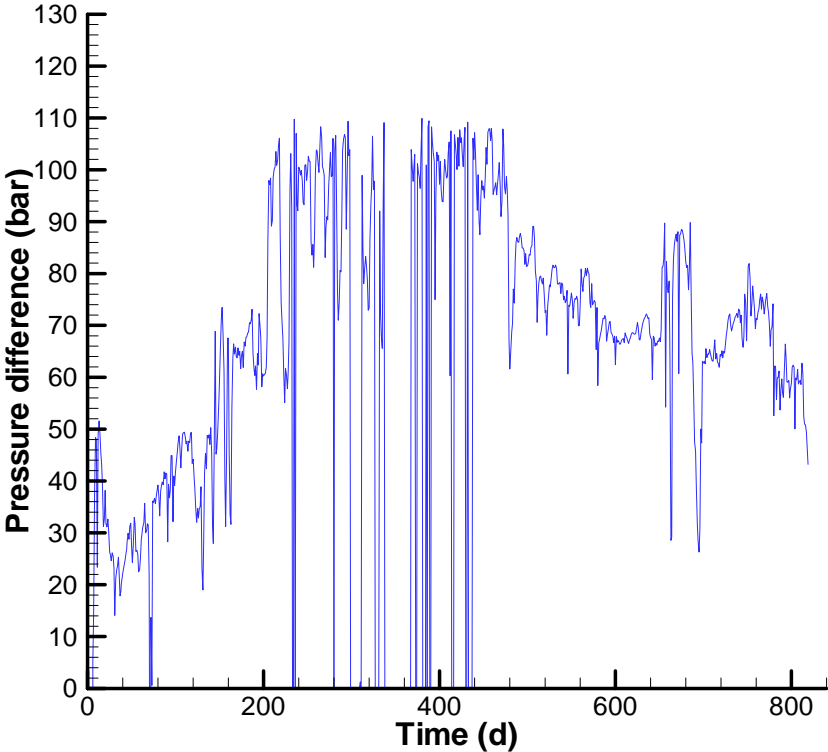
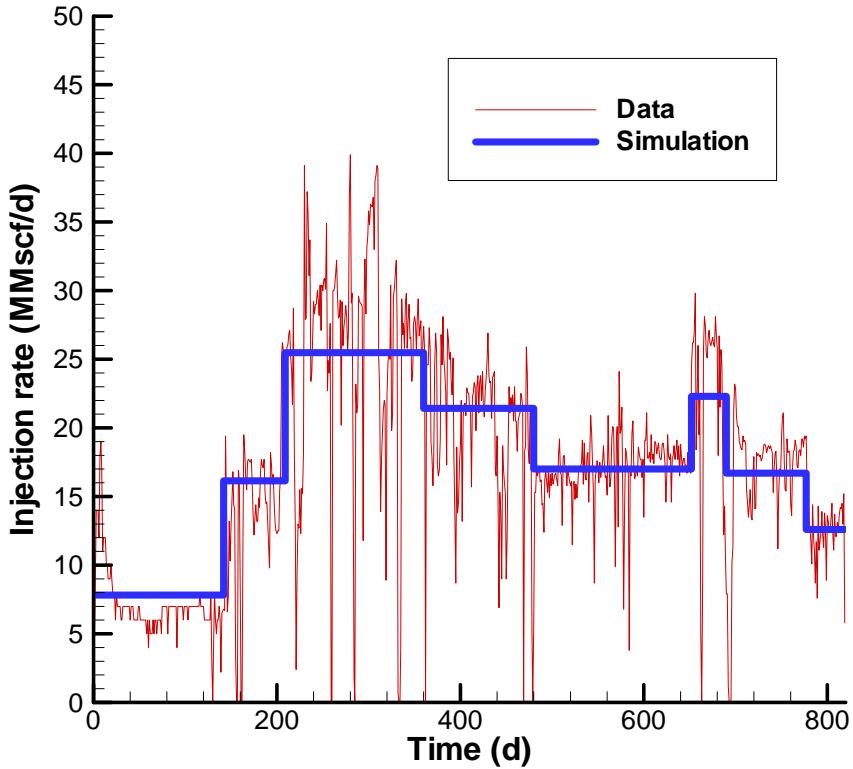
Model Development



Wright (2008)

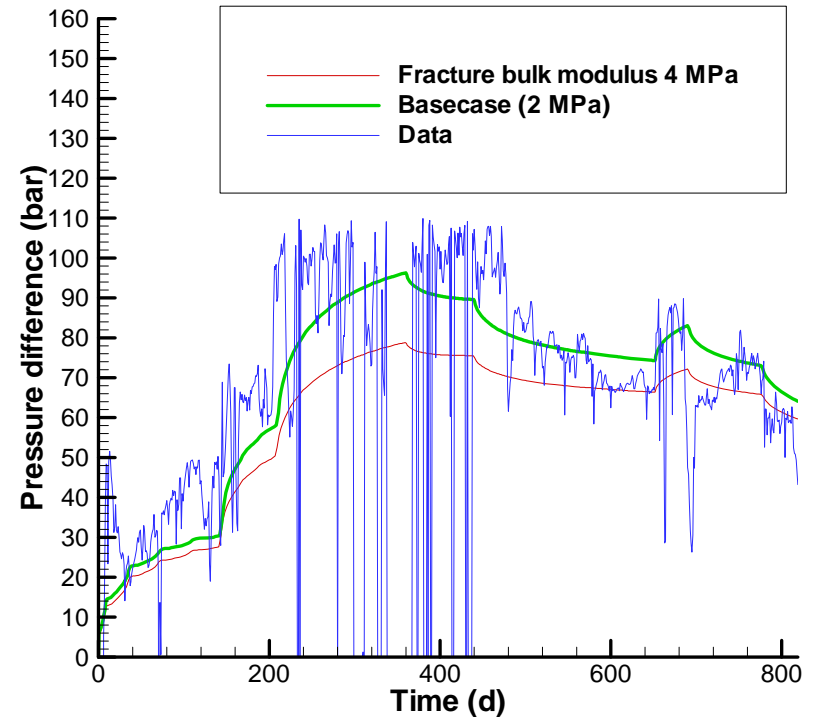
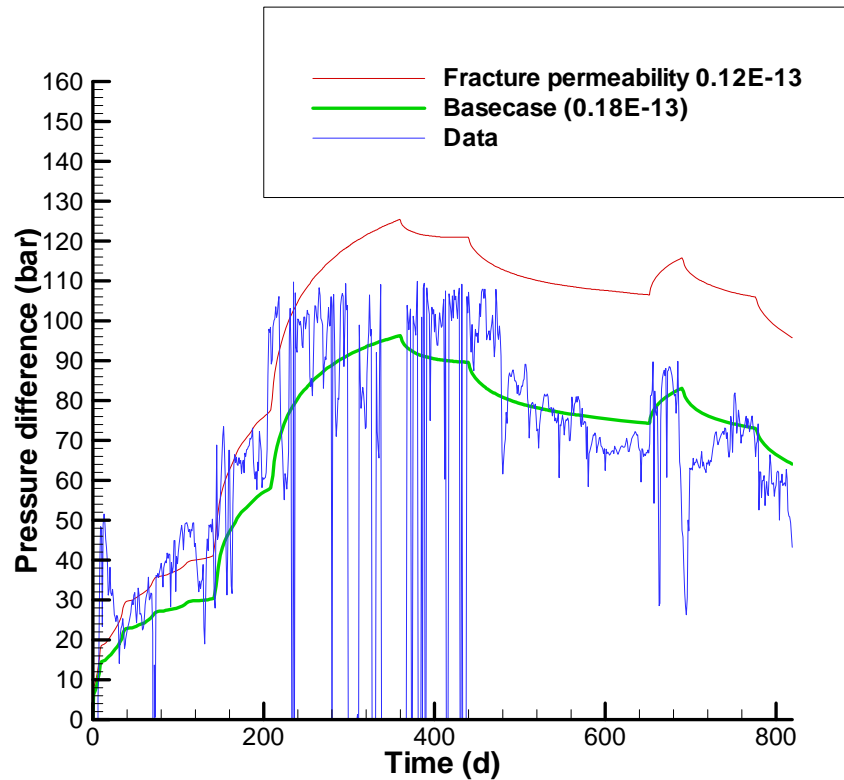


Simulation of injection at In Salah: Data Use



Simulation of injection at In Salah:

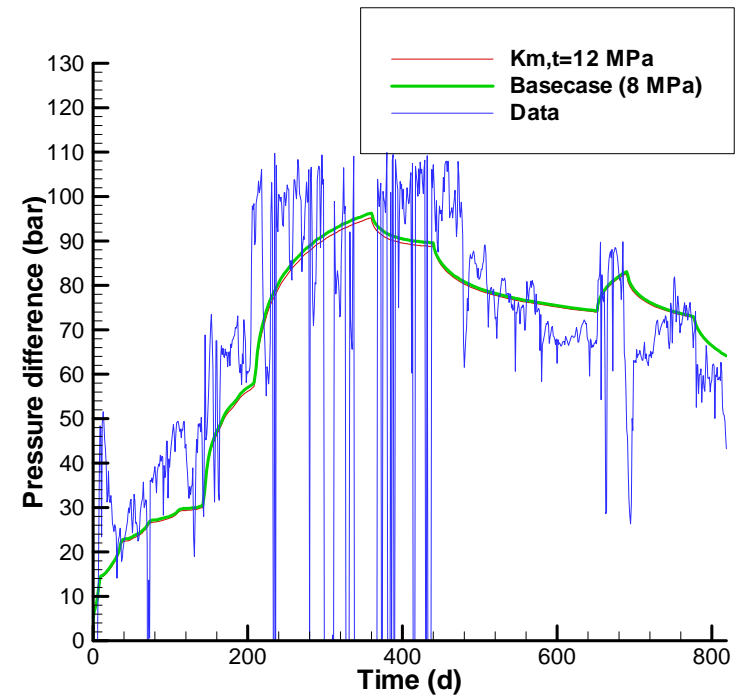
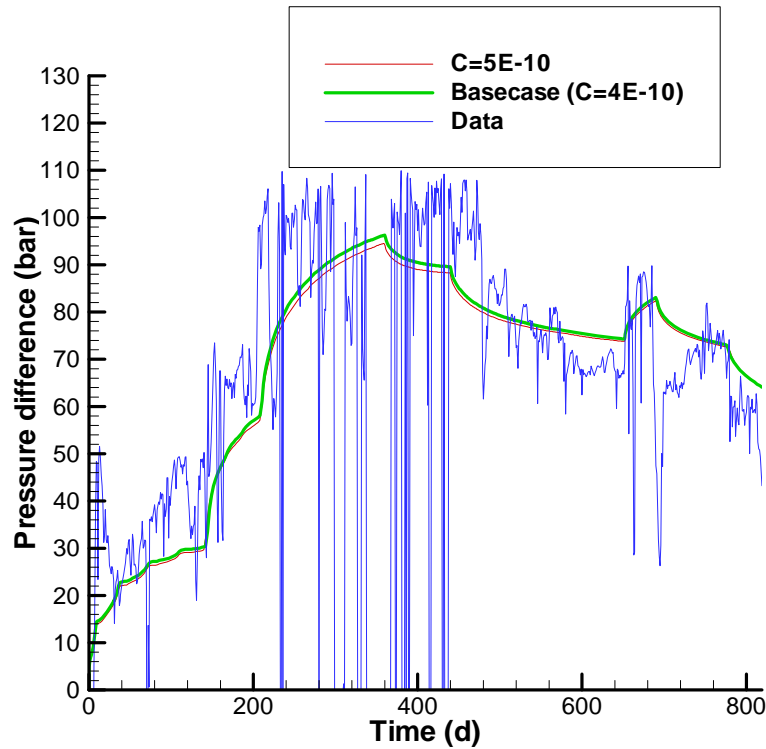
Sensitivity Study of Fracture Properties



$$b \approx b_{0,e} + b_{0,t} \exp\left(-\frac{\sigma}{K_{F,t}}\right)$$

Simulation of injection at In Salah:

Sensitivity Study of Matrix Properties



$$\phi = \phi_e (1 - C \sigma) + \gamma_t \exp\left(-\frac{\sigma}{K_{m,t}}\right)$$

Conclusions

- A dual-continuum approach for coupled hydro-mechanical has been developed for modeling CO₂ geological sequestration at In Salah.
- The governing equation for liquid flow includes an additional storage term owing to effects of rock deformation.
- Coupled hydro-mechanical process plays an important role in determining CO₂ injectivity.
- Fracture properties have significant effects on CO₂ injection process at the In Salah site.

Acknowledgement

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